Direct Sequence Spread Spectrum:

**Aim:**
Introduction to Direct sequence spread spectrum.

**Introduction:**
In some situations it is required that a communication signal be difficult to detect, and difficult to demodulate even when detected. Here the word ‘detect’ is used in the sense of ‘to discover the presence of’. The signal is required to have a low probability of intercept - LPI.

In other situations a signal is required that is difficult to interfere with, or ‘jam’. The ‘spread spectrum’ signal has properties which help to achieve these ends. Spread spectrum signals may be divided into two main groups - direct sequence spread spectrum (DSSS), and frequency hopping spread spectrum (FHSS). This experiment is concerned with demonstrating some of the principles of the first.

**Principle of DSSS:**
Consider the frequency translation of a baseband message (of bandwidth $B$ Hz) to a higher part of the spectrum, using DSBSC modulation. The resulting signal occupies a bandwidth of $2B$ Hz, and would typically override the noise occupying the same part of the spectrum. This makes it easy to find with a spectrum analyser (for example), and so the probability of intercept is high. A local carrier, synchronized with that at the transmitter, is required at the receiver for synchronous demodulation. The recovered signal-to-noise ratio is 3 dB better than that measured at its original location in the spectrum. This 3 dB improvement comes from the fact that the contributions from each sideband add coherently, whereas the noise does not. This can be called a 3 dB ‘processing gain’, and is related to the fact that the transmission bandwidth and message bandwidth are in the ratio of 2:1.

In a spread spectrum system literally thousands of different carriers are used, to generate thousands of DSBSC signals each derived from the same message. These carriers are spread over a wide bandwidth (much wider than $2B$ Hz), and so the resulting DSBSC signals will be spread over the same bandwidth.

If the total transmitted power is similar to that of the single DSBSC case, then the power of an individual DSBSC in the spread spectrum case is thousands of times less. In fact, over the bandwidth occupied by one of these DSBSC signals, it would be literally ‘buried in the noise’, and difficult to find with a spectrum analyser (for example).

Instead of the total transmitted power being concentrated in a band of width $2B$ Hz, the multiple carriers have spread it thinly over a very wide bandwidth. The signal-to-noise ratio for each DSBSC is very low (well below 0 dB). To recover the message from the
transmitted spread spectrum signal all that a receiver requires is thousands of local carriers, at the same frequency and of the same relative phase, as all those at the transmitter. All these carriers come from a pseudo random binary sequence (PRBS) generator.

Given a stable clock, and a long sequence, it may be shown that the spectrum of a pseudo random binary sequence generator is a good source of these carriers. A second PRBS generator, of the same type, clocked at the same rate, and appropriately aligned, is sufficient to regenerate all the required local carriers at the receiver demodulator.

In the spread spectrum context the PRBS signal is generally called a PN – pseudo noise - signal, since its spectrum approaches that of random noise.

Having the correct sequence at the receiver means that the message contributions from each of the thousands of minute DSBSC signals combine in phase – coherently - and add up to a finite message output. Otherwise they add with random phases, resulting in a (very) small, noise-like output.

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\text{The key to a successful message recovery is the knowledge of the PN sequence used at the transmitter.}
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**Processing gain:**

To achieve most of the claims made for the spread spectrum it is necessary that the bandwidth over which the message is spread be very much greater than the bandwidth of the message itself. Each DSBSC of the DSSS signal is at a level below the noise, but each is processed by the synchronous demodulator to give a 3 dB SNR improvement. The total improvement is proportional to the number of individual DSBSC components. In fact the processing gain of the system is equal to the ratio of DSSS bandwidth to message bandwidth.

**A DSSS generator:**

To generate a spread spectrum signal one requires:

1. A modulated signal somewhere in the RF spectrum
2. A PN sequence to spread it
These two are combined as shown in Figure 1.

![Figure 1: basis of spread spectrum](image)

There are two bandwidths involved here: that of the modulated signal, and the spreading sequence. The first will be very much less than the second. The output spread spectrum signal will be spread either side of the original RF carrier ($\omega_0$) by an amount equal to the bandwidth of the PN sequence.

Most of the energy of the sequence will lie in the range DC to $\omega_s$, where $\omega_s$ is the sequence clock. The longer the sequence the more spectral components will lie in this range. It is necessary and usual that $\omega_0 >\gg \omega_s$, although in the experiment to follow the difference will not be large.

The modulated signal can be of any type, but typically digitally-derived, such as binary phase shift keyed - BPSK. In this case the arrangement of Figure 1 can be expanded to that of Figure 2.

A digital message is preferred in an operational spread spectrum system, since it makes the task of the eavesdropper even more difficult.

![Figure 2: a spread BPSK signal](image)
The arrangement of Figure 2 can be simplified by noting that, if the clock of the bipolar message is a sub-multiple of the clock of the PN sequence, then the modulotwo sum of the message and the PN sequence can be used to multiply the RF carrier, generating a DSSS signal with a single multiplier. Such a simplification will not be implemented in this experiment.

**A DSSS demodulator:**

A demodulator for the DSSS of Figure 1 is shown in block form in Figure 3.

![DSSS Demodulator Diagram](image)

**Figure 3: DSSS demodulator**

The input multiplier performs the de-spreading of the received signal, and the second multiplier translates the modulated signal down to baseband. The filter output would probably require further processing - not shown - to ‘clean up’ the waveform to binary format.

The PN sequence at the receiver acts as a ‘key’ to the transmission. It must not only have the same clock and bit pattern; it must be **aligned** properly with the sequence at the transmitter.

**The PN spectrum:**

The PN signal, being periodic, has a line spectrum. This spectrum is determined by the PN clock period $T_c$ and the sequence length $N$ (the number of bits, or clock periods, before the pattern repeats).

- the spectral lines are separated by $(1/NT_c)$ Hz.
- there is a DC component of amplitude $(1/N)$.
- the amplitude of an individual line in the spectrum is weighted, where:

  $$\text{weight} = \sqrt{\frac{2(N+1)}{N^2} \left( \frac{\sin(m/N)}{m/N} \right)^2 }, \quad n \neq 0$$
It is clear that a plot of these weights will show them lying within an envelope having a sync function shape. Most of the energy of the PN sequence lies below the first minimum (when n = N); that is, below the clock frequency.

For approximate analysis it is often assumed that the shape of the power spectral density is rectangular, extending from DC to (1/Tc) Hz.

**Experimental Procedure:**

This experiment will be concerned with modelling the systems of Figures 2 and 3.

**The message:**

The message comes from a SEQUENCE GENERATOR. To obtain a reasonable processing gain the message clock needs to be much slower than the PN clock. Being a sub-multiple of the PN clock is also an advantage. The 2 kHz MESSAGE from the MASTER SIGNALS module has been used - 1/48 of the 100 kHz master clock. You may prefer a larger division ratio. This can be achieved with further division using the DIGITAL UTILITIES module.

Select a short message sequence for stable oscilloscope displays (both toggles of the on-board switch UP).

**The transmission medium:**

The transmitter is connected to the receiver via an ADDER, acting as a nonbandlimiting (and so no delay) transmission path. The second input to the ADDER will be used for inserting noise. The inclusion of a finite delay would introduce problems with aligning the receiver PN sequence.

**Clocks:**

Since the PN clock is a sub-multiple of the carrier, only one of these needs to be recovered by the receiver. In the experiment they are stolen from the transmitter.

**Generation:**

_T1 model the block diagram of Figure 2. This is shown in Figure 4. The ADDER is included for inserting noise from a NOISE GENERATOR (module not shown)._
T2 before inserting the SEQUENCE GENERATOR modules, select a short sequence for the message (both toggles of the on-board switch SW2 UP), and the same long sequence for the PN generators (both toggles of the on-board switch SW2 DOWN).

T3 initially use the 100 kHz TTL available from MASTER SIGNALS, divided by 12, using a DIGITAL UTILITIES module (not shown), for the PN generator clock.

T4 initially reduce the noise output from the ADDER to zero.

T5 instead of connecting the bi-polar message sequence to the X input of the first MULTIPLIER, connect instead the 2 kHz MESSAGE (sinusoidal) signal. This makes the output from the first MULTIPLIER a DSBSC signal, easily recognisable on the oscilloscope. Check this.

T6 instead of connecting the PN sequence to the X input of the second MULTIPLIER, connect instead the VARIABLE DC module set to near +2 volt. This makes the second MULTIPLIER a voltage controlled amplifier with a gain of about unity. Thus the ‘DSSS output’ will be a well-recognisable DSBSC based on a 2 kHz message. Check your levels with this recognisable signal.

T7 using the SPECTRUM ANALYSER, examine the output spectrum. Confirm it is a DSBSC.

When satisfied that the MULTIPLIER modules are behaving as expected, return their inputs to the signals previously connected.

T8 synchronize the oscilloscope to the SYNCH signal (START-OF-SEQUENCE) of the message generator. Examine signals throughout the system. Some will be familiar, others not. There are no adjustments to be made, except for the output amplitude from the ADDER.

T9 using the SPECTRUM ANALYSER, examine the output spectrum. With an 8.333 kHz PN clock, confirm that the output spectrum - the DSSS signal - has its energy concentrated over about 8 kHz either side of the 100 kHz carrier.
**T10** now add noise. Adjust the noise level so that, while observing the spectrum of the ADDER output, the DSSS signal can be seen above the noise level.

**T11** while still observing the spectrum, increase the spread of the DSSS signal. This is done by increasing the PN sequence clock rate by choosing a lower division of the 100 kHz TTL - choose divide-by-2, for a 50 kHz clock.

The increase of PN clock rate has widened the spectrum of the PN sequence to about 50 kHz (from 8 kHz). Since the DSSS signal contains the same energy as before, it has been spread more thinly over the spectrum, and it will have sunk deeper into, and got ‘lost’ in, the noise.

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\text{This is one of the main purposes of spread spectrum.}
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**Demodulation:**

**T12** model the receiver of Figure 3 as suggested in Figure 5 below. Both the 100 kHz carrier, and the PN sequence, are stolen from the transmitter. Not shown is a PHASE SHIFTER for the 100 kHz carrier. This is used to maximize the output amplitude (it will also change its polarity).

**T13** the bandwidth of the output filter is chosen to suit the message. Use a TUNEABLE LPF (shown in Figure 5), or the 3 kHz LPF in the HEADPHONE AMPLIFIER. For restoration of the output to a TTL format a DECISION MAKER would be included, but this is not necessary for this experiment. Visual comparison of the sent and received sequences is adequate.

![Figure 5: the receiver model](image)

Although there are two stolen clocks shown, in practice it is often only necessary to acquire, by what ever means, a single clock. This is because one can be a known sub-multiple of the other.
**T14** observe the output, when the transmitter is connected to the input. Probably there will be ‘nothing’ - or nothing resembling the expected output sequence. Varying the phase of the 100 kHz carrier should not change things.

The problem is that the receiver PN sequence, although synchronized with that at the transmitter, is not correctly aligned in time. With no transmission delay it is a simple matter to achieve this.

**T15** bring the two sequences into alignment by momentarily connecting the start-of-sequence **SYNC** output of the transmitter **SEQUENCE GENERATOR** to the **RESET** input of the receiver **SEQUENCE GENERATOR**.

**T16** re-examine the output from the demodulator. The message should have been recovered (being a short sequence, this is easy to confirm visually). Adjust the bandwidth of the demodulator output filter for minimum bandwidth consistent with reasonable waveshape. Remember, a DECISION MAKER could be used to regenerate a perfect copy of the original, but this is not necessary for our present purpose.

**Interference:**

**T17** with the system set up and showing the demodulated sequence at the receiver output, replace the noise with a 100 kHz sinusoid from a VCO. This represents an interfering signal (a very elementary form of jamming). Monitor the VCO with the **FREQUENCY COUNTER**.

**T18** while watching the demodulator output, sweep the VCO frequency through its full frequency range.

| the wanted sequence will still be present at the demodulator output, but there will be negligible sign of the effects of the interfering signal. You have demonstrated another important property of spread spectrum. |
Discussion Question:

1) Consider a DSBSC signal derived from a single tone. How many lines would there be in the spectrum of the spread signal? You will have to supply some data regarding the spreading sequence.

2) Consider a DSBSC signal derived from a single tone. How many lines would there be in the de-spread spectrum? You will have to supply some data regarding the spreading sequence.

3) What advantage is there in making the message bit rate a sub-multiple of the PN bit rate?

4) Explain the principle of operation involved in CDMA?