



# *Digital Integrated Circuits*

## *A Design Perspective*

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# Introduction

*July 30, 2002*

# *What is this book all about?*

## □ **Introduction to digital integrated circuits.**

- CMOS devices and manufacturing technology. CMOS inverters and gates. Propagation delay, noise margins, and power dissipation. Sequential circuits. Arithmetic, interconnect, and memories. Programmable logic arrays. Design methodologies.

## □ **What will you learn?**

- Understanding, designing, and optimizing digital circuits with respect to different quality metrics: cost, speed, power dissipation, and reliability

# s *Digital Integrated Circuits*

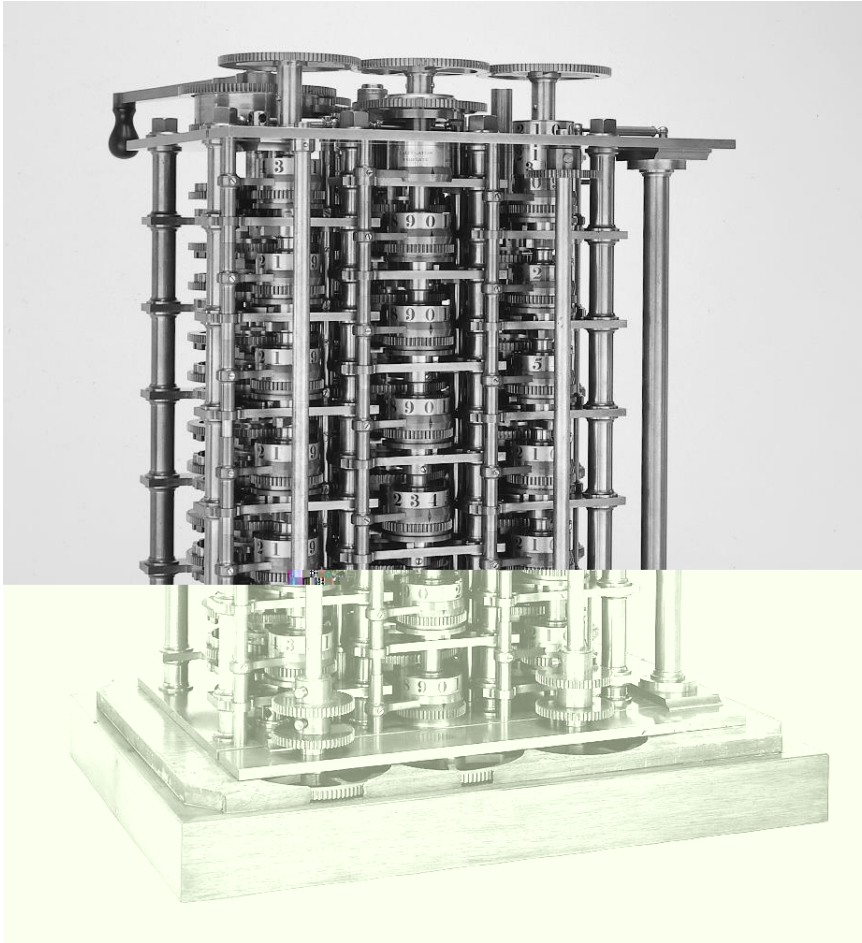
- ❑ Introduction: Issues in digital design
- ❑ The CMOS inverter
- ❑ Combinational logic structures
- ❑ Sequential logic gates
- ❑ Design methodologies
- ❑ Interconnect: R, L and C
- ❑ Timing
- ❑ Arithmetic building blocks
- ❑ Memories and array structures

# Introduction

- ❑ Why is designing digital ICs different today than it was before?
- ❑ Will it change in future?



# *The First Computer*



**The Babbage  
Difference Engine  
(1832)**

**25,000 parts**

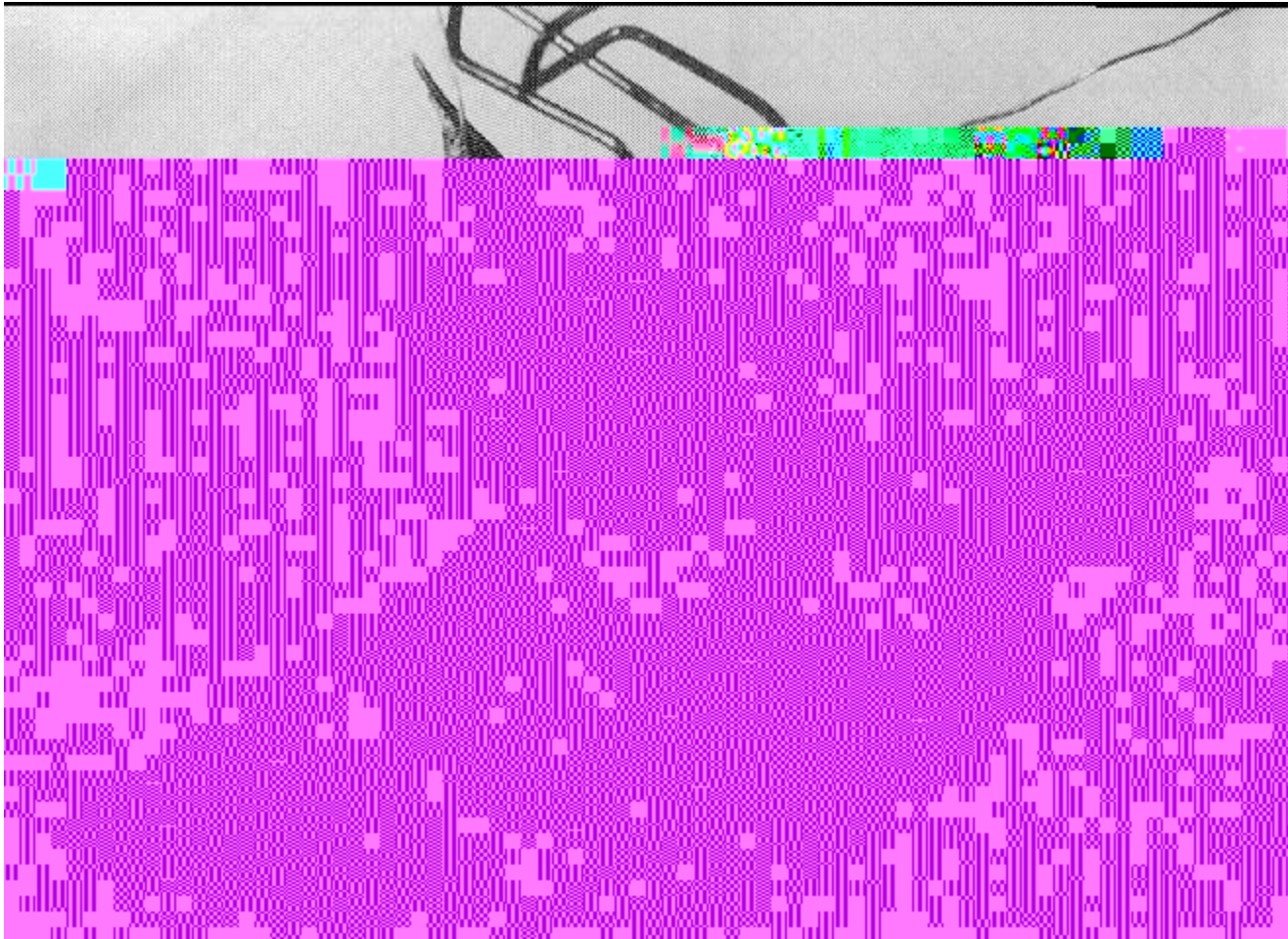
**cost: £17,470**



# *ENIAC - The first electronic computer (1946)*

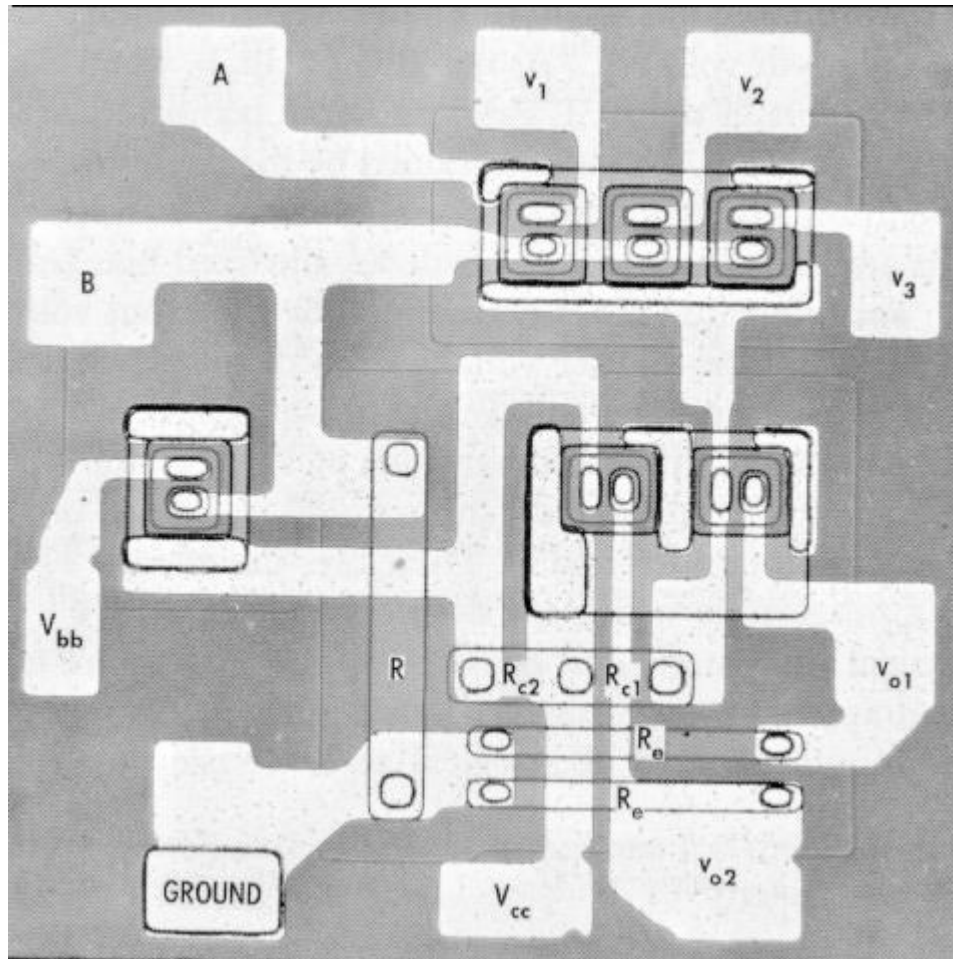


# The Transistor Revolution



First transistor  
Bell Labs, 1948

# The First Integrated Circuits

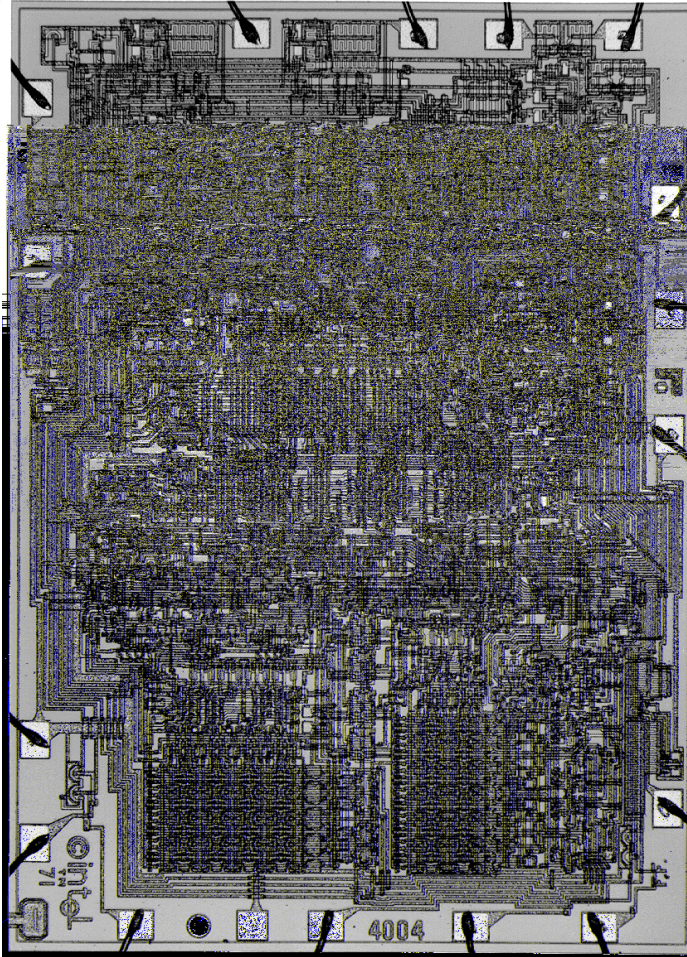


*Bipolar logic*  
*1960's*

ECL 3-input Gate  
Motorola 1966



# Intel 4004 Micro-Processor

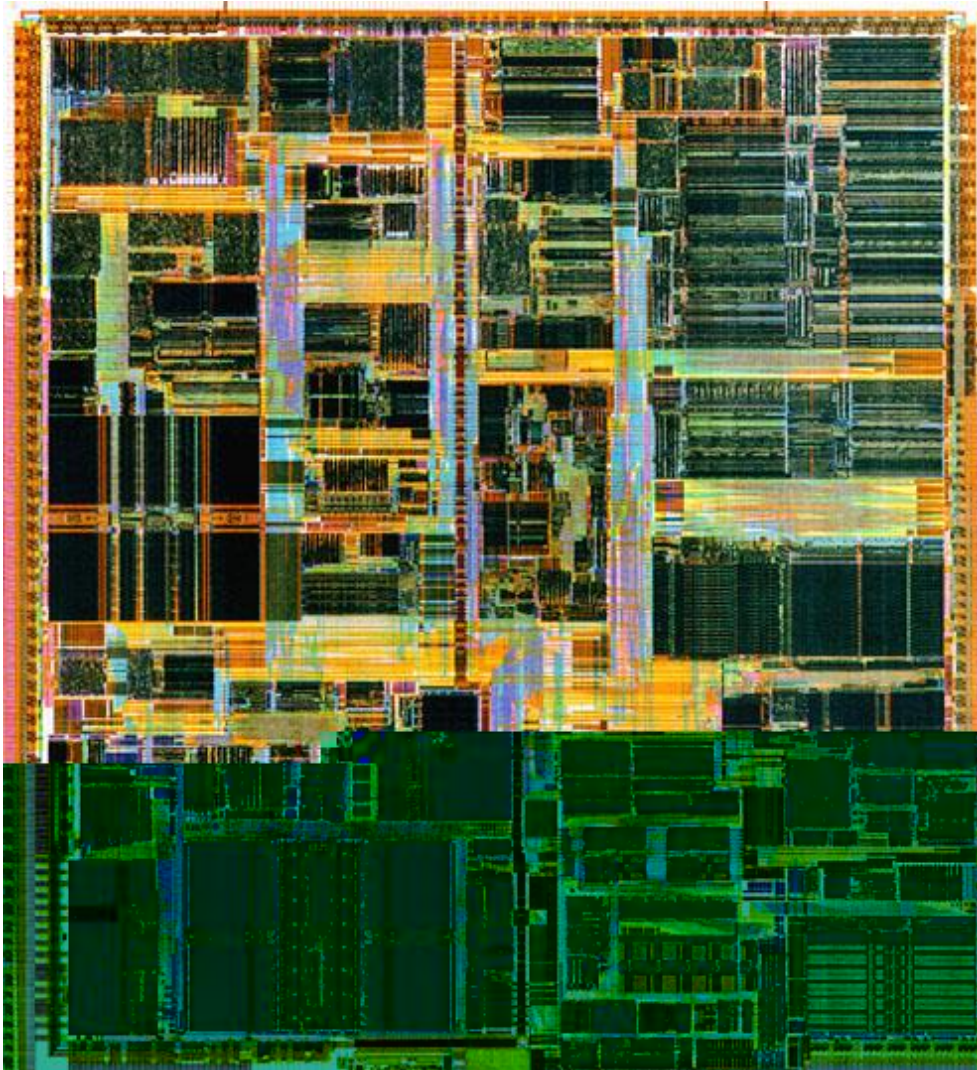


1971

1000 transistors

1 MHz operation

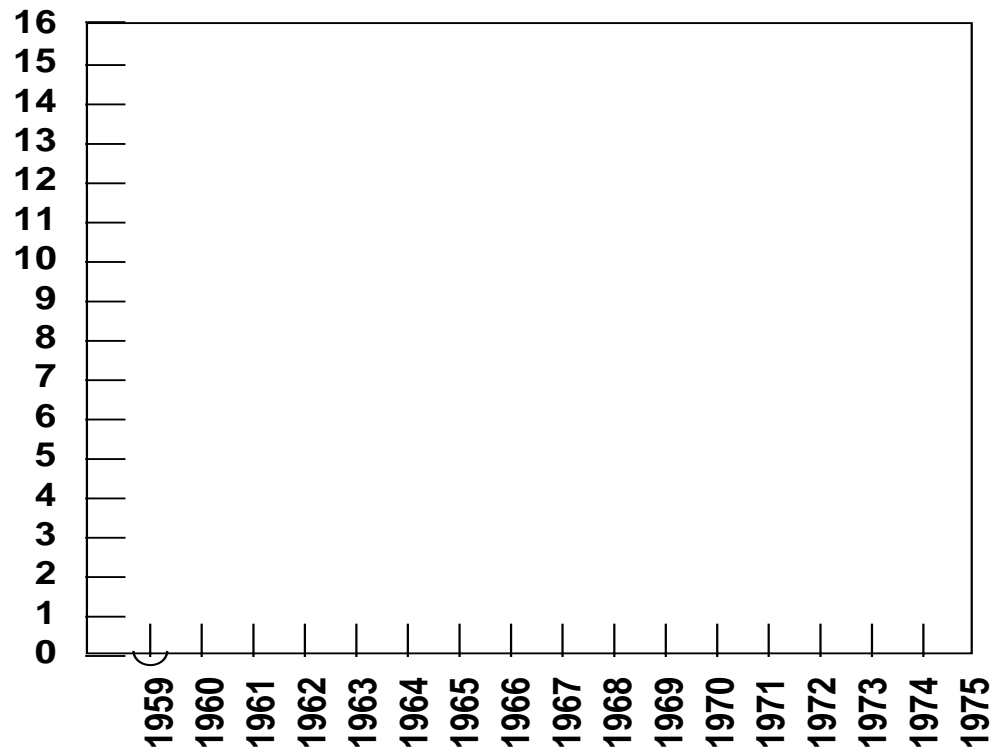
# *Intel Pentium (IV) microprocessor*



# Moore's Law

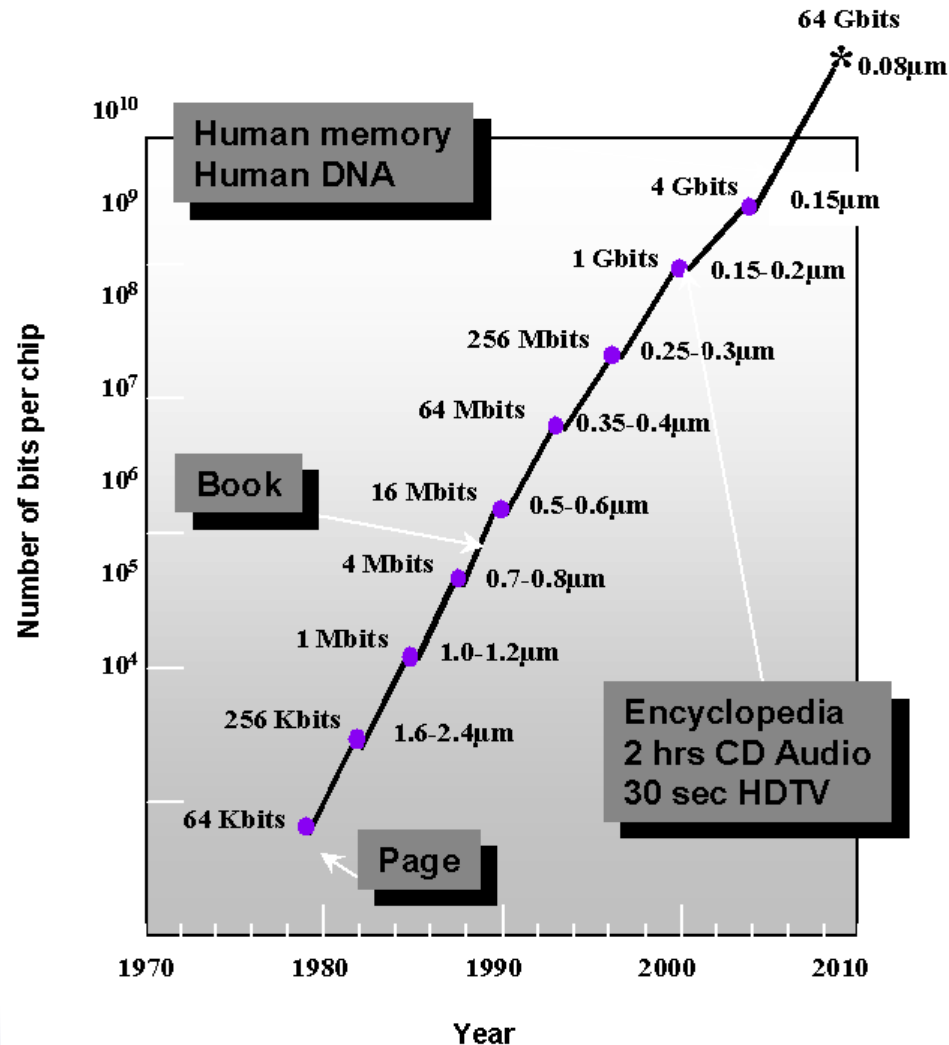
- In 1965, Gordon Moore noted that the number of transistors on a chip doubled every 18 to 24 months.
- He made a prediction that semiconductor technology will double its effectiveness every 18 months

# Moore's Law



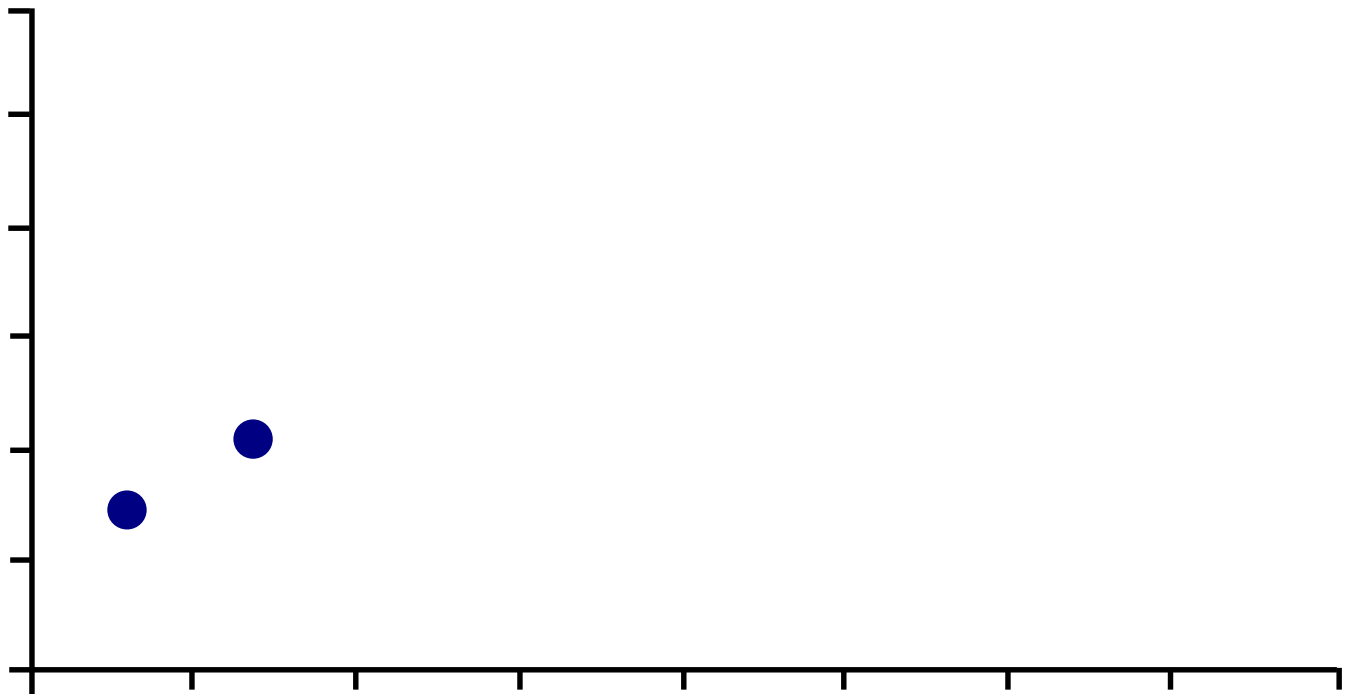
*Electronics, April 19, 1965.*

# Evolution in Complexity

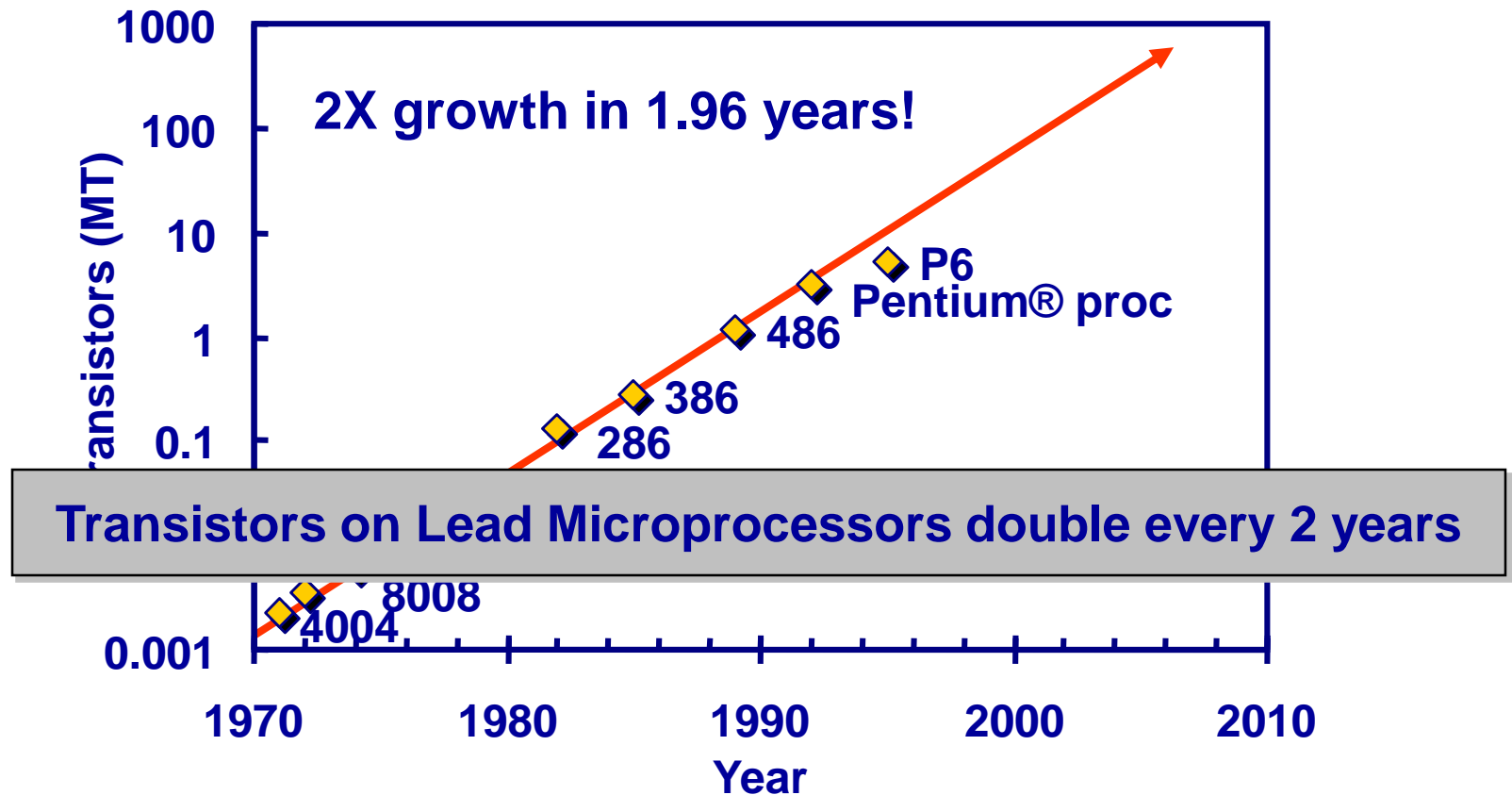




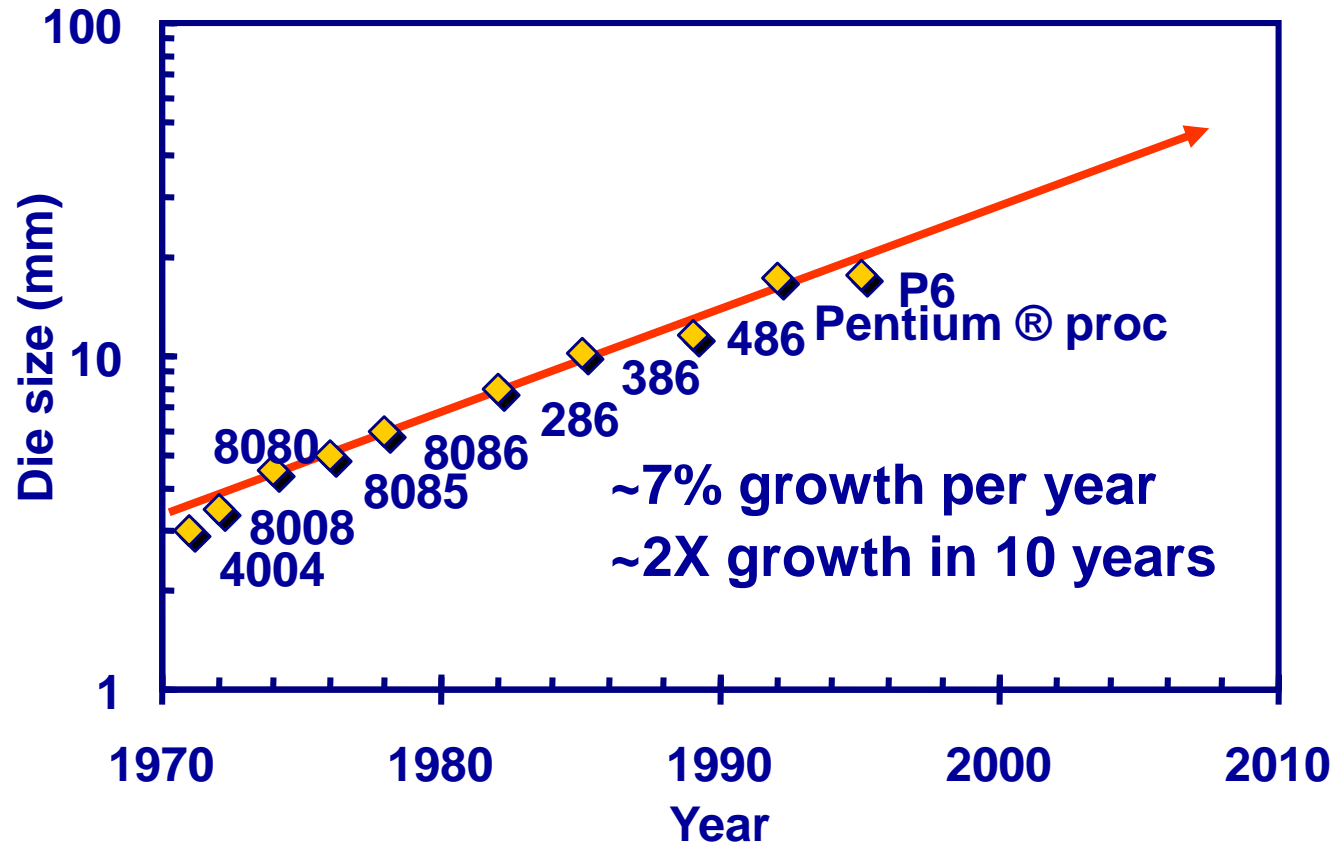
# *Transistor Counts*



# Moore's law in Microprocessors

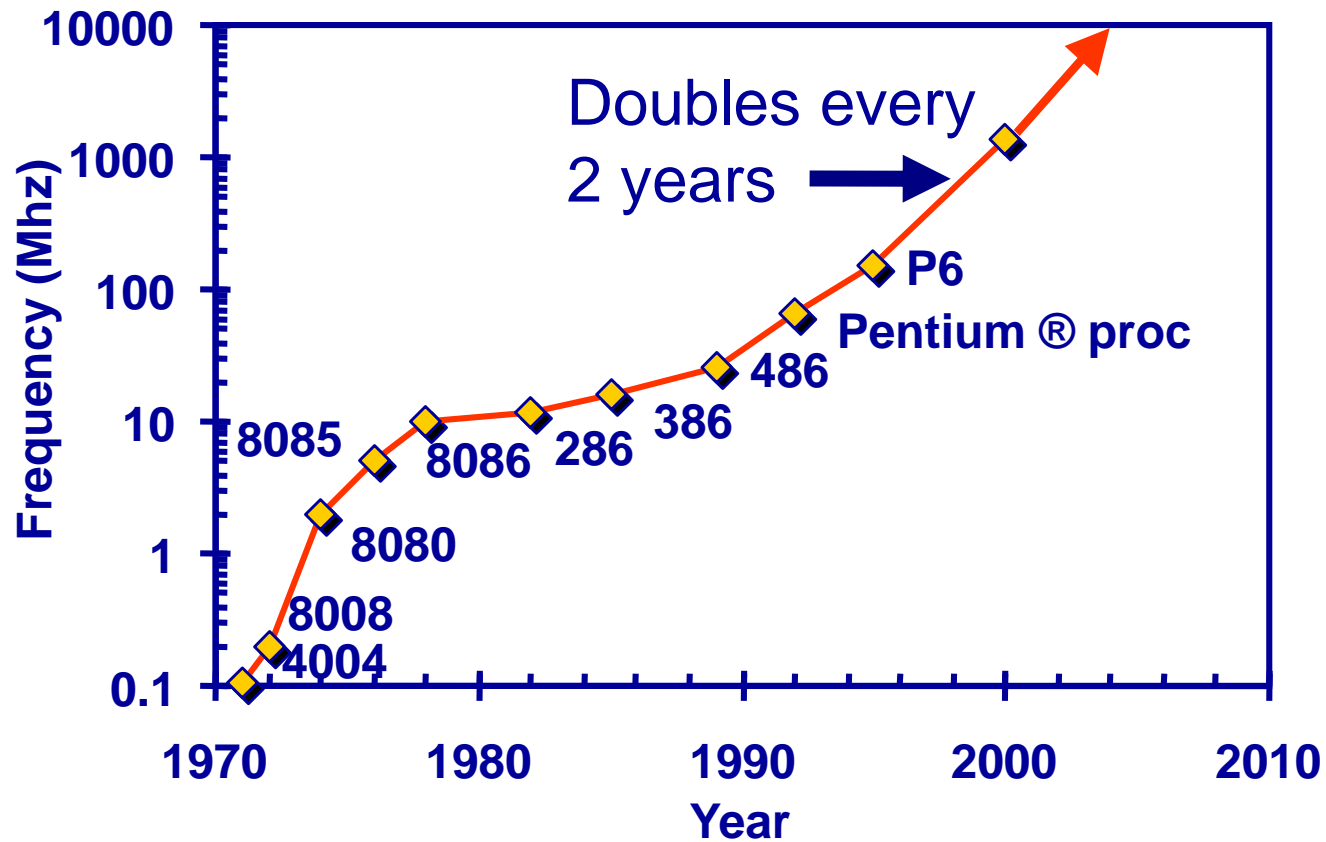


# Die Size Growth



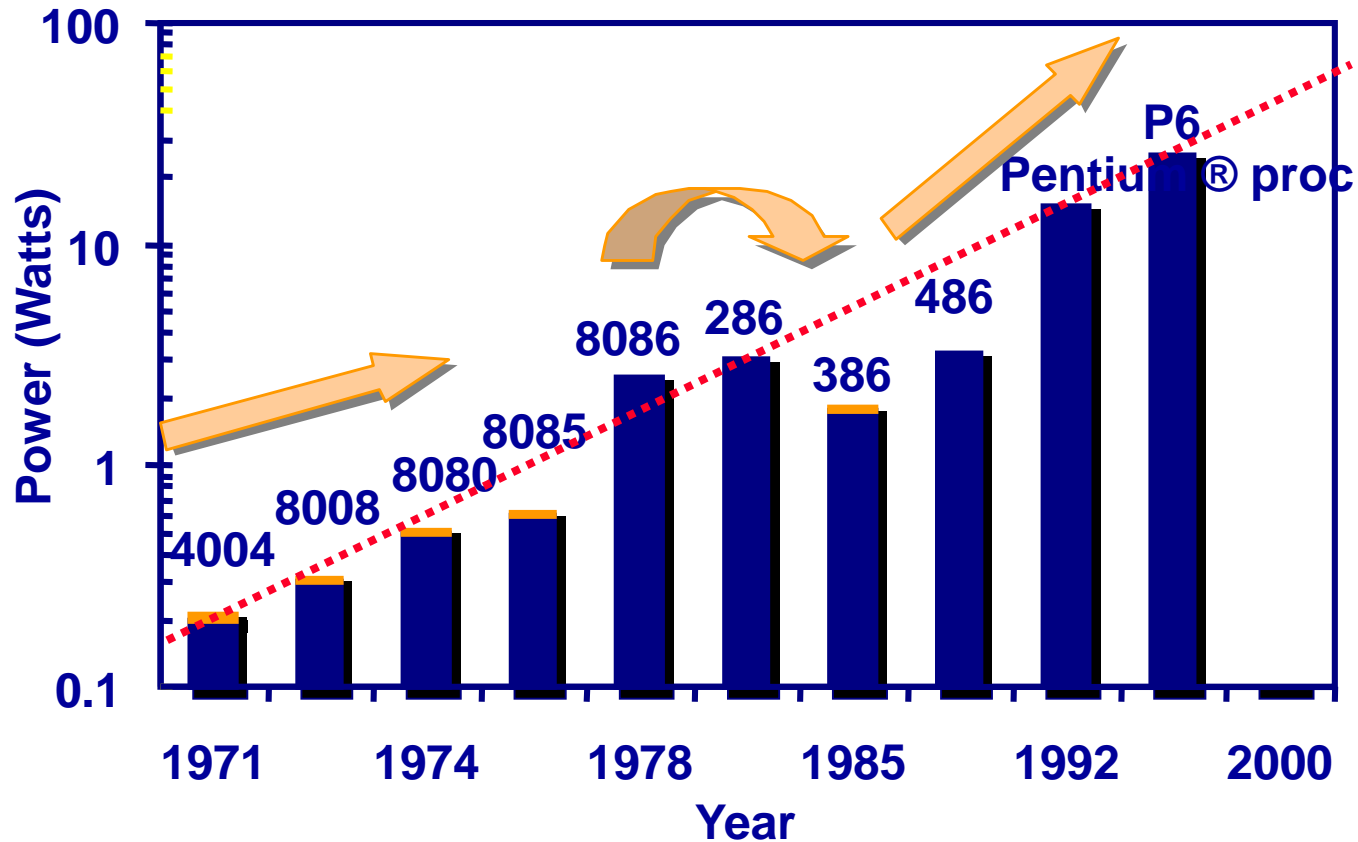
Die size grows by 14% to satisfy Moore's Law

# Frequency



**Lead Microprocessors frequency doubles every 2 years**

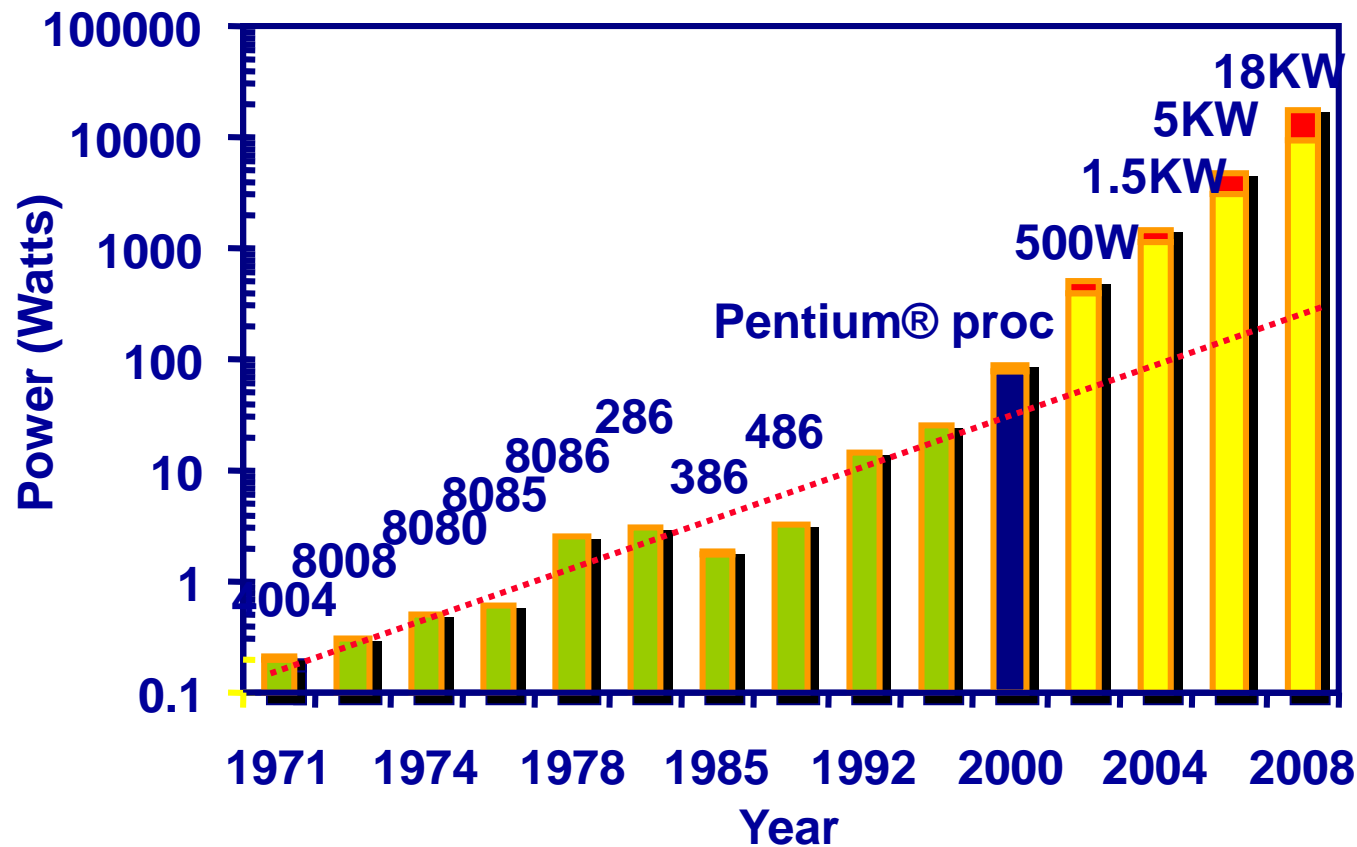
# Power Dissipation



**Lead Microprocessors power continues to increase**

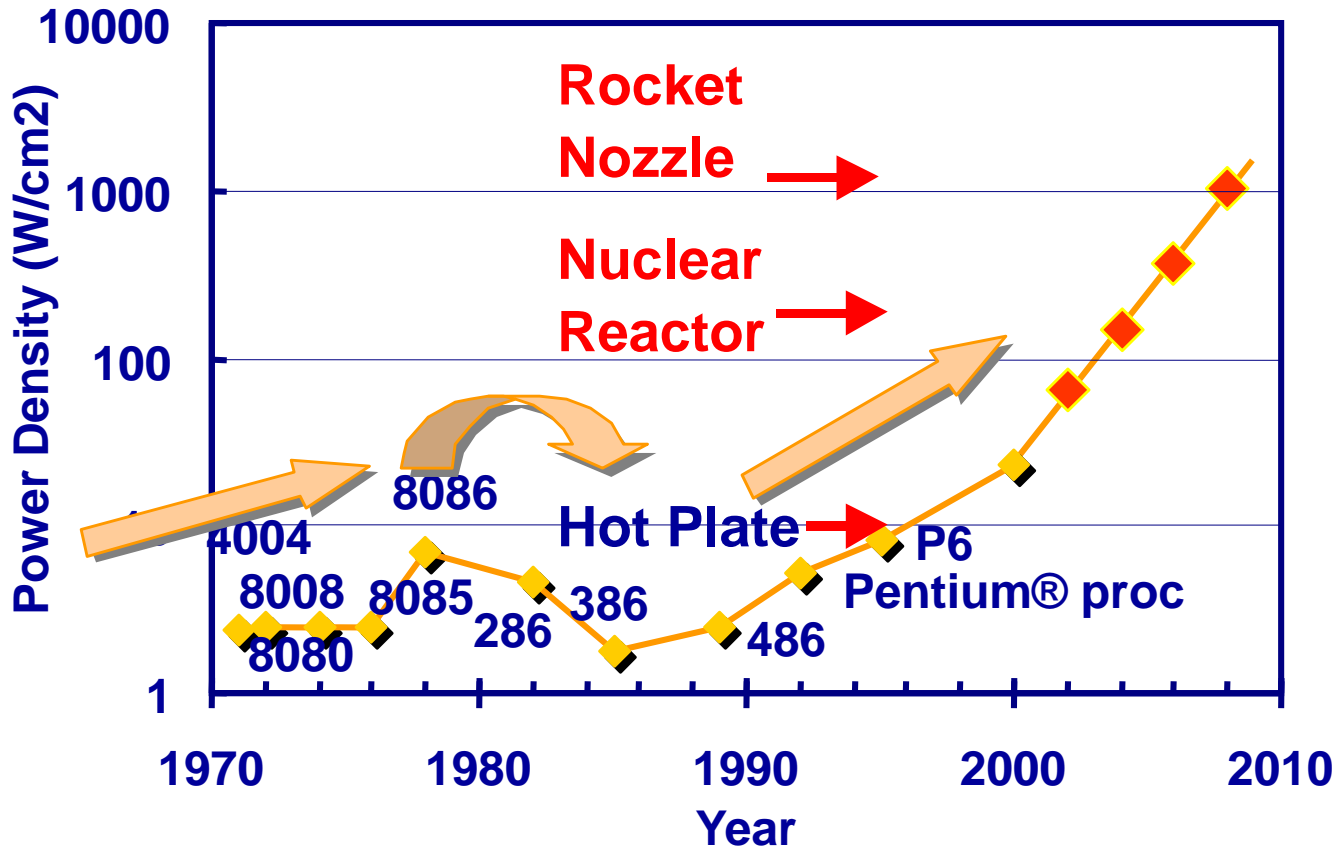


# *Power will be a major problem*



**Power delivery and dissipation will be prohibitive**

# Power density



Power density too high to keep junctions at low temp

# Not Only Microprocessors

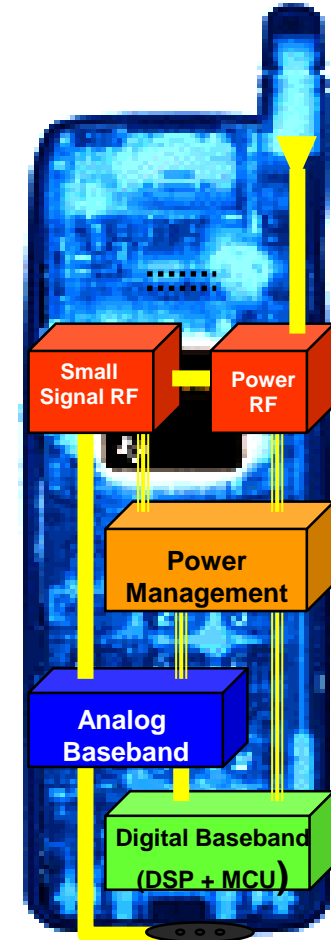
## Cell Phone



### Digital Cellular Market (Phones Shipped)

	1996	1997	1998	1999	2000
Units	48M	86M	162M	260M	435M

(data from Texas Instruments)

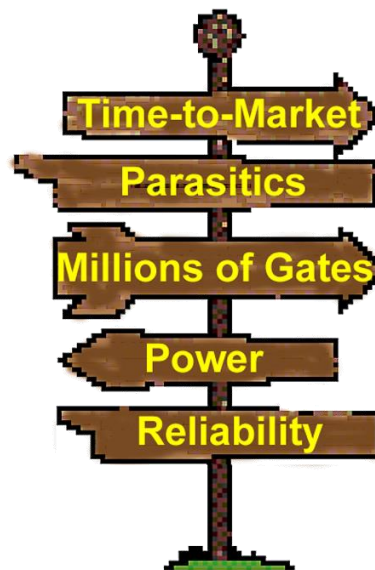


# Challenges in Digital Design

$\propto$  DSM

## “Microscopic Problems”

- Ultra-high speed design
- Interconnect
- Noise, Crosstalk
- Reliability, Manufacturability
- Power Dissipation
- Clock distribution.



$\propto$  1/DSM

## “Macroscopic Issues”

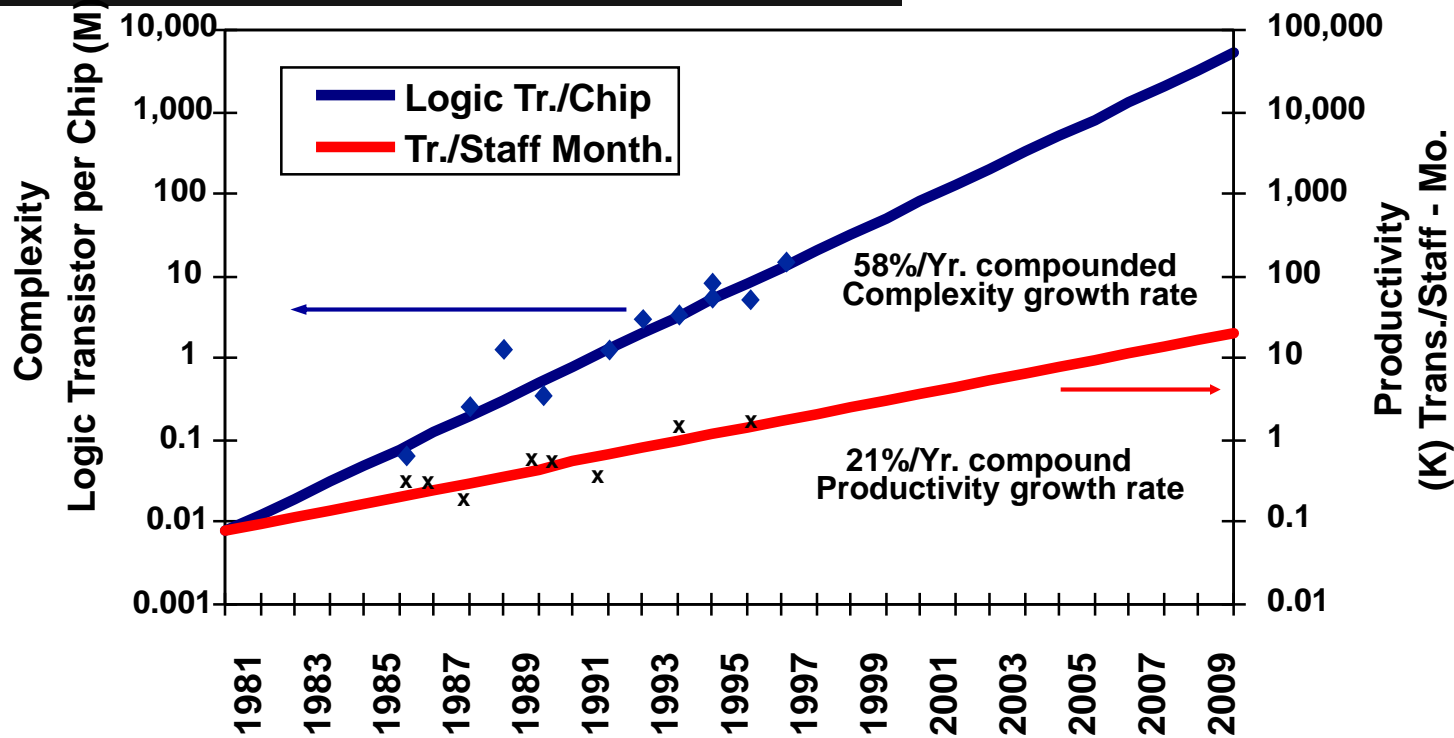
- Time-to-Market
- Millions of Gates
- High-Level Abstractions
- Reuse & IP: Portability
- Predictability
- etc.

Everything Looks a Little Different

?

...and There's a Lot of Them!

# Productivity Trends



Source: Sematech

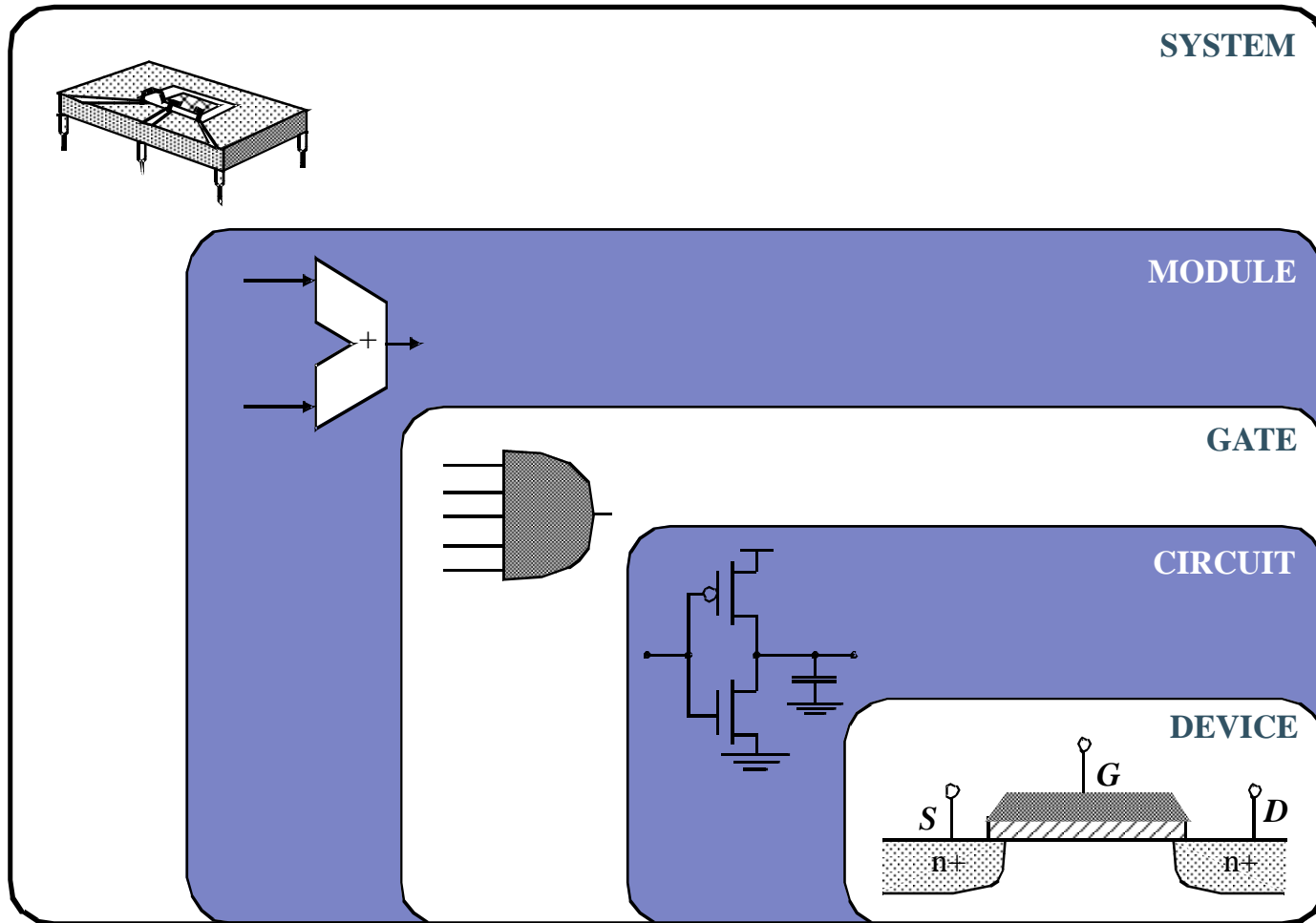
**Complexity outpaces design productivity**



# Why Scaling?

- ❑ Technology shrinks by 0.7/generation
- ❑ With every generation can integrate 2x more functions per chip; chip cost does not increase significantly
- ❑ Cost of a function decreases by 2x
- ❑ But ...
  - How to design chips with more and more functions?
  - Design engineering population does not double every two years...
- ❑ Hence, a need for more efficient design methods
  - Exploit different levels of abstraction

# Design Abstraction Levels



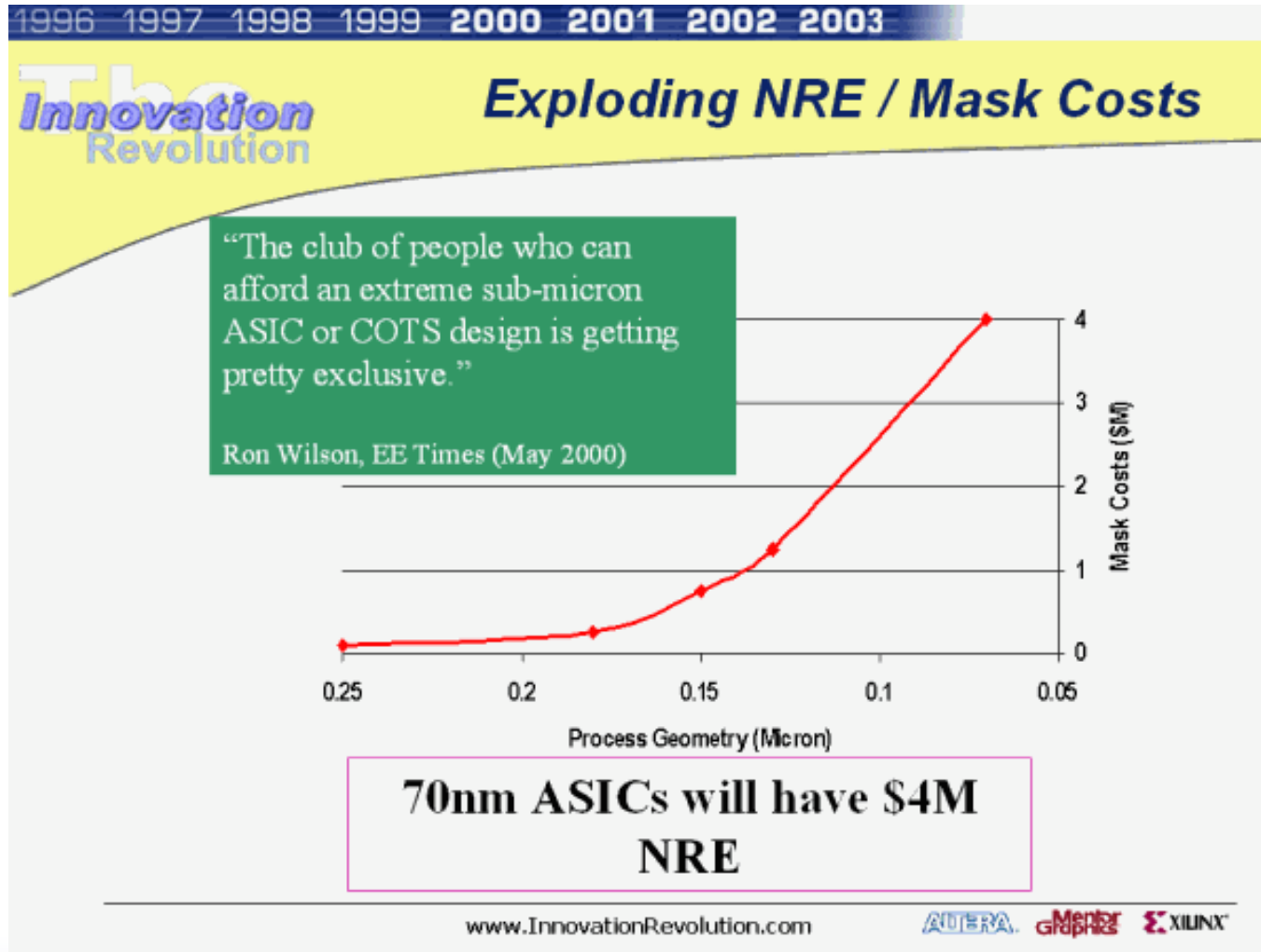
# *Design Metrics*

- How to evaluate performance of a digital circuit (gate, block, ...)?
  - Cost
  - Reliability
  - Scalability
  - Speed (delay, operating frequency)
  - Power dissipation
  - Energy to perform a function

# Cost of Integrated Circuits

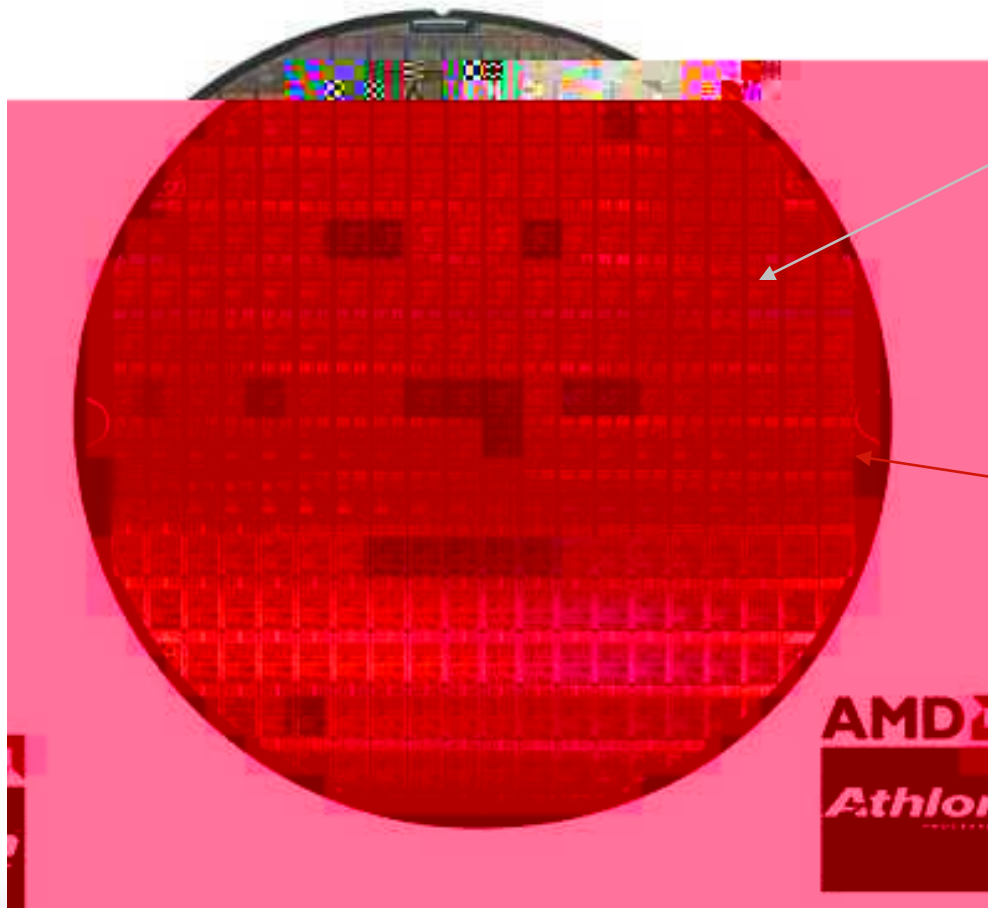
- ❑ NRE (non-recurrent engineering) costs
  - design time and effort, mask generation
  - one-time cost factor
- ❑ Recurrent costs
  - silicon processing, packaging, test
  - proportional to volume
  - proportional to chip area

# NRE Cost is Increasing





# Die Cost



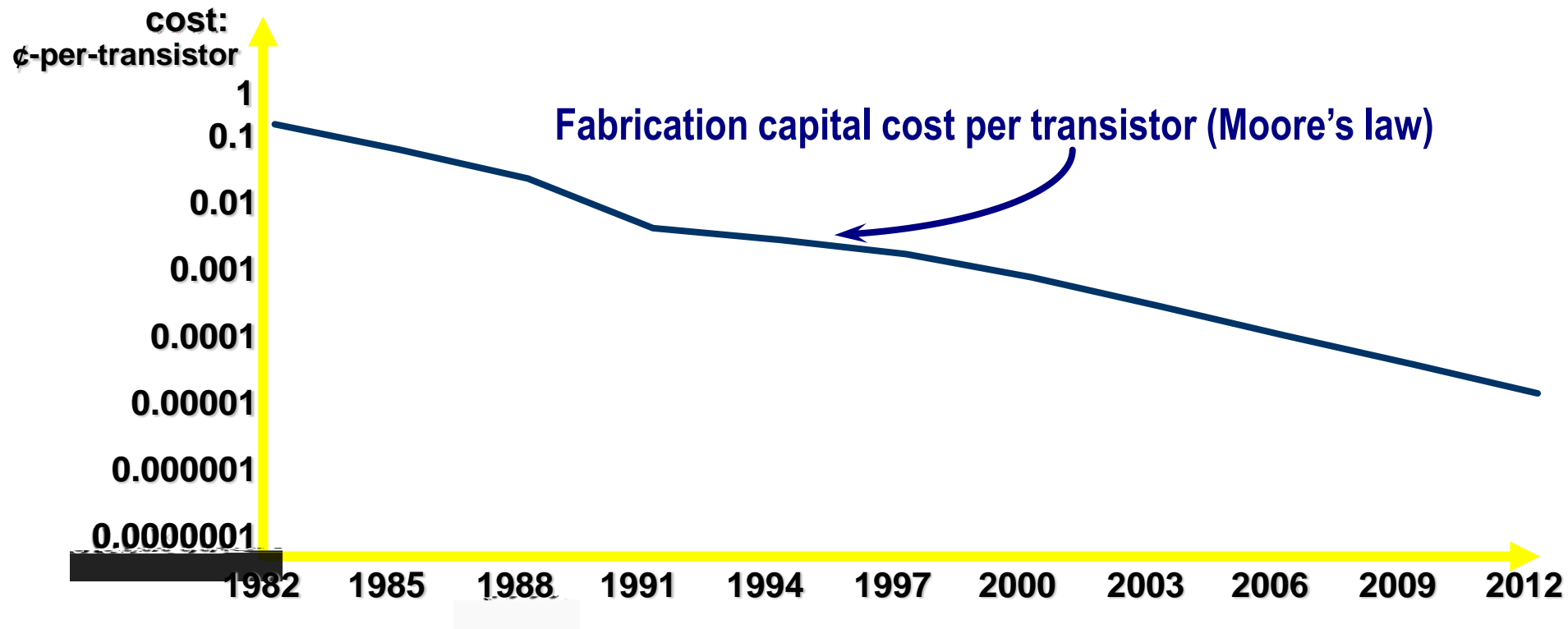
Single die

Wafer

Going up to 12" (30cm)

From <http://www.amd.com>

# Cost per Transistor

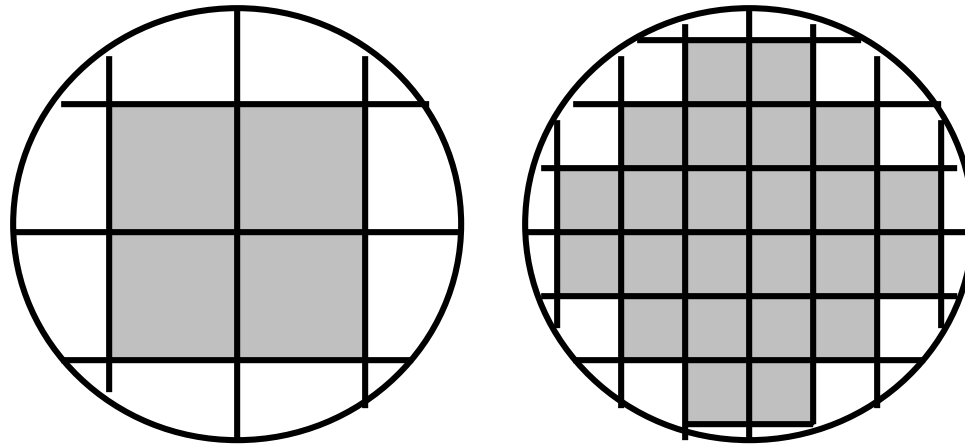


# Yield

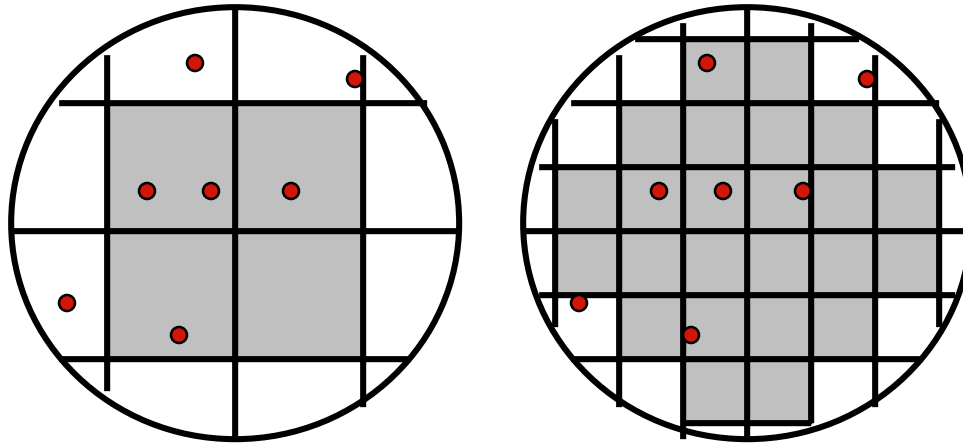
$$Y = \frac{\text{No. of good chips per wafer}}{\text{Total number of chips per wafer}} \times 100\%$$

$$\text{Die cost} = \frac{\text{Wafer cost}}{\text{Dies per wafer} \times \text{Die yield}}$$

$$\text{Dies per wafer} = \frac{\pi \times (\text{wafer diameter}/2)^2}{\text{die area}} - \frac{\pi \times \text{wafer diameter}}{\sqrt{2} \times \text{die area}}$$



# Defects



$$\text{die yield} = \left( 1 + \frac{\text{defects per unit area} \times \text{die area}}{\alpha} \right)^{-\alpha}$$

$\alpha$  is approximately 3

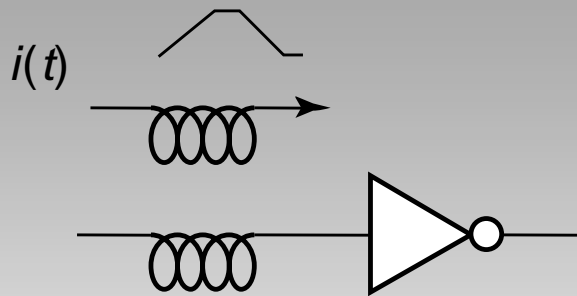
$$\text{die cost} = f(\text{die area})^4$$

# Some Examples (1994)

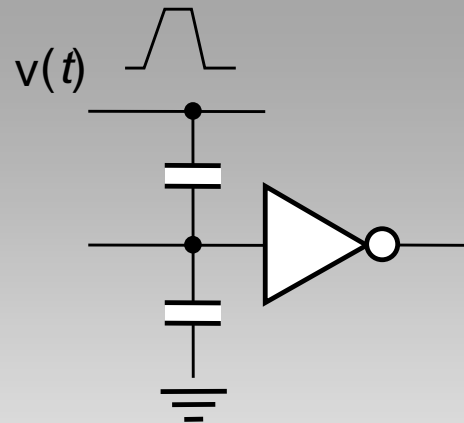
Chip	Metal layers	Line width	Wafer cost	Def./cm <sup>2</sup>	Area mm <sup>2</sup>	Dies/wafer	Yield	Die cost
386DX	2	0.90	\$900	1.0	43	360	71%	\$4
486 DX2	3	0.80	\$1200	1.0	81	181	54%	\$12
Power PC 601	4	0.80	\$1700	1.3	121	115	28%	\$53
HP PA 7100	3	0.80	\$1300	1.0	196	66	27%	\$73
DEC Alpha	3	0.70	\$1500	1.2	234	53	19%	\$149
Super Sparc	3	0.70	\$1700	1.6	256	48	13%	\$272
Pentium	3	0.80	\$1500	1.5	296	40	9%	\$417

# Reliability—

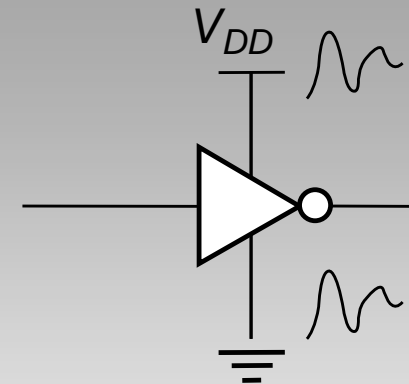
## Noise in Digital Integrated Circuits



**Inductive coupling**



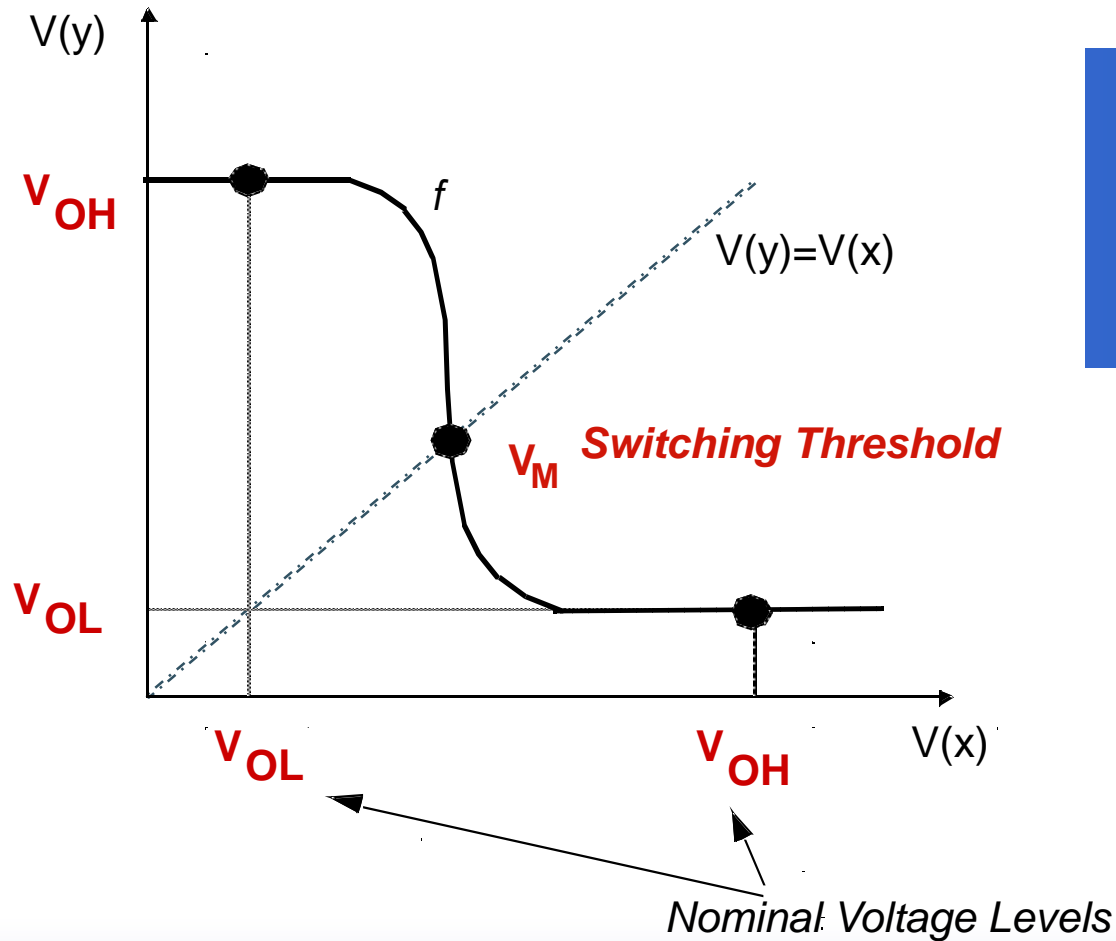
**Capacitive coupling**



**Power and ground noise**

# DC Operation

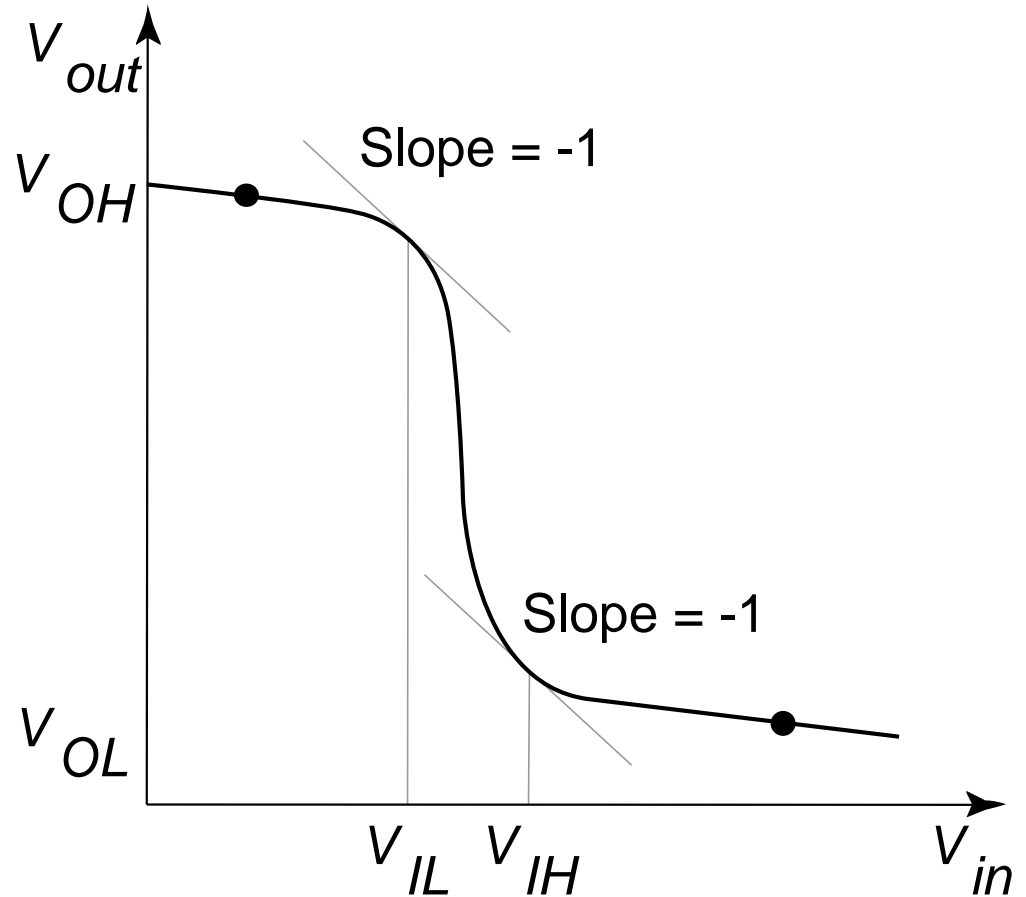
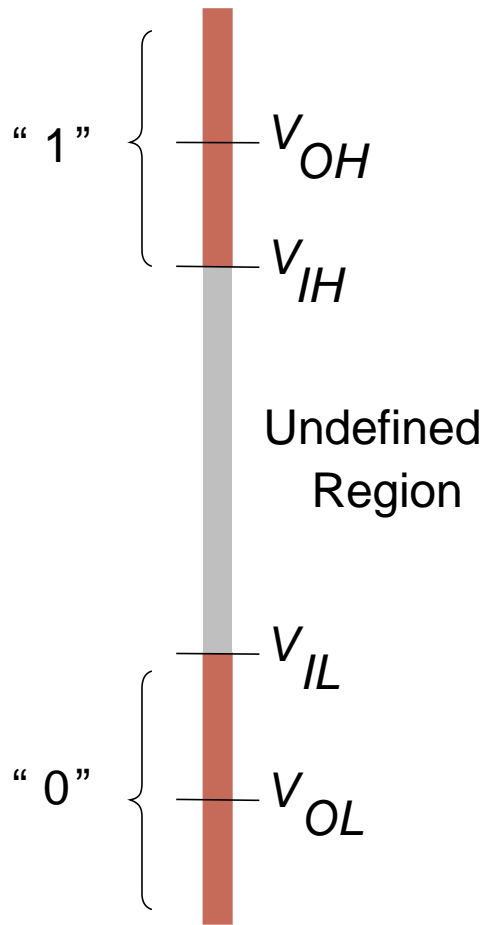
## Voltage Transfer Characteristic



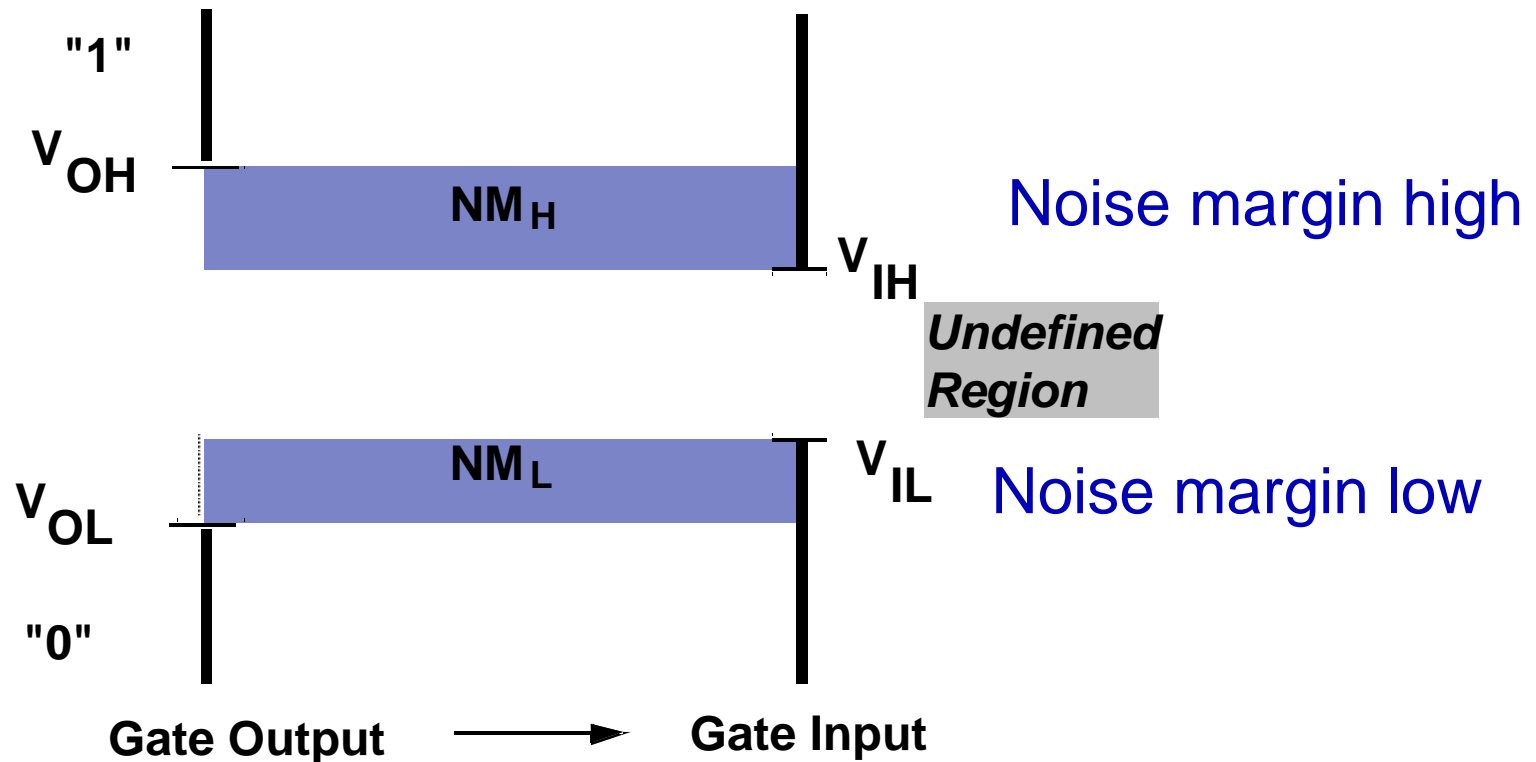
$$\begin{aligned} V_{OH} &= f(V_{OL}) \\ V_{OL} &= f(V_{OH}) \\ V_M &= f(V_M) \end{aligned}$$



# Mapping between analog and digital signals



# Definition of Noise Margins



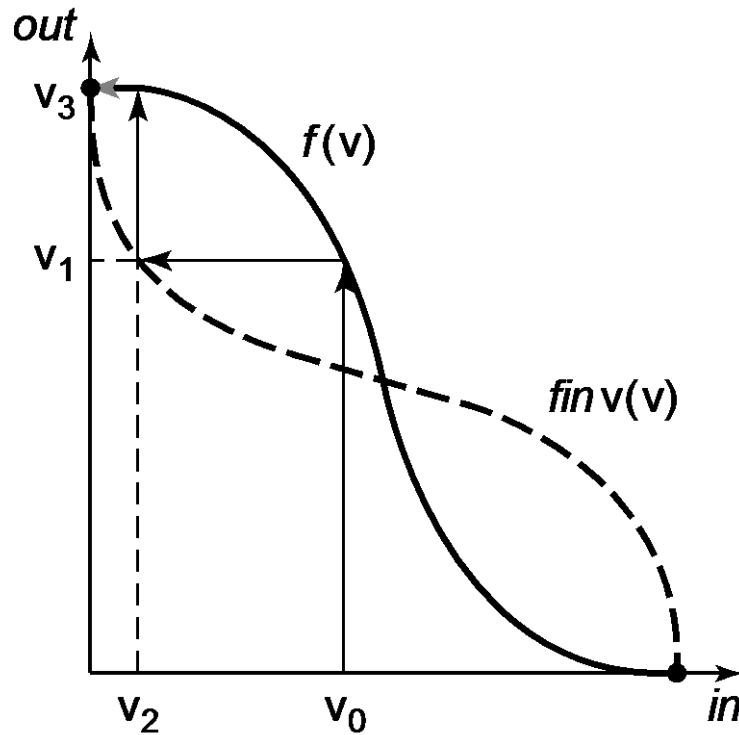
# *Noise Budget*

- ❑ Allocates gross noise margin to expected sources of noise
- ❑ Sources: supply noise, cross talk, interference, offset
- ❑ Differentiate between fixed and proportional noise sources

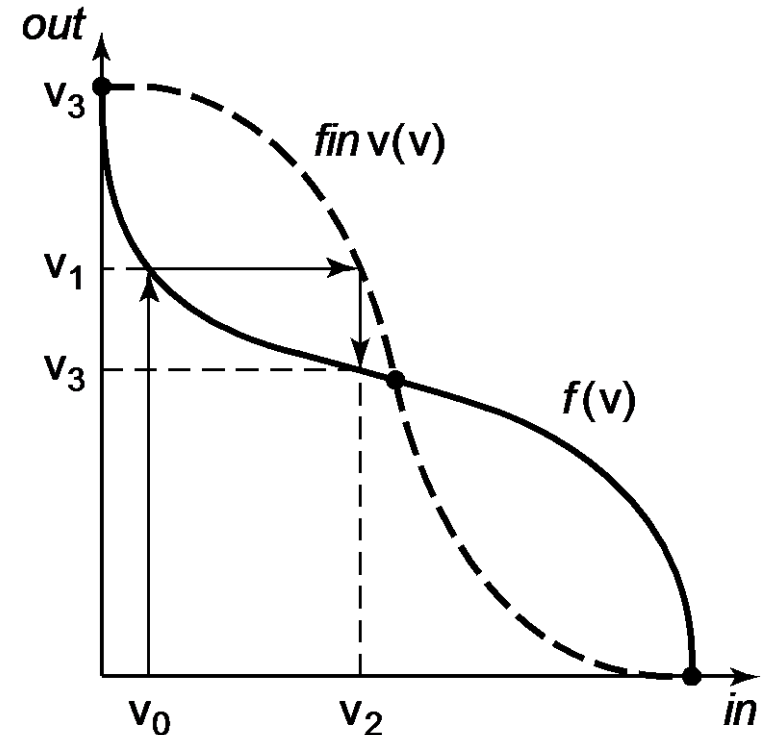
# Key Reliability Properties

- ❑ Absolute noise margin values are deceptive
  - a floating node is more easily disturbed than a node driven by a low impedance (in terms of voltage)
- ❑ Noise immunity is the more important metric –  
**the capability to suppress noise sources**
- ❑ Key metrics: Noise transfer functions, Output impedance of the driver and input impedance of the receiver;

# Regenerative Property

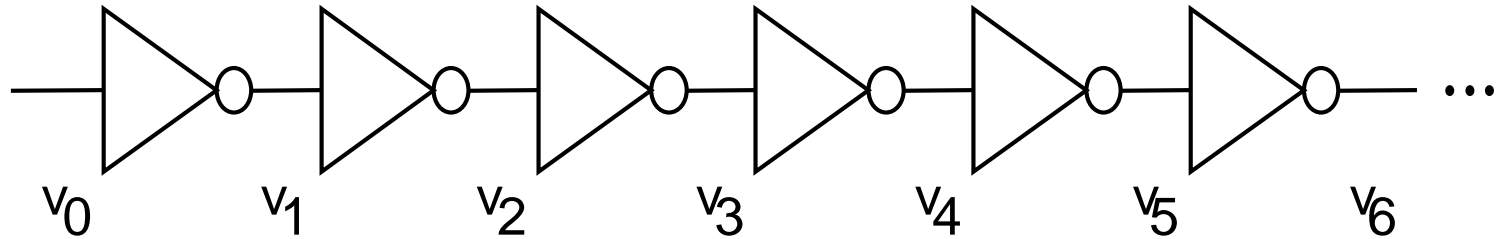


Regenerative

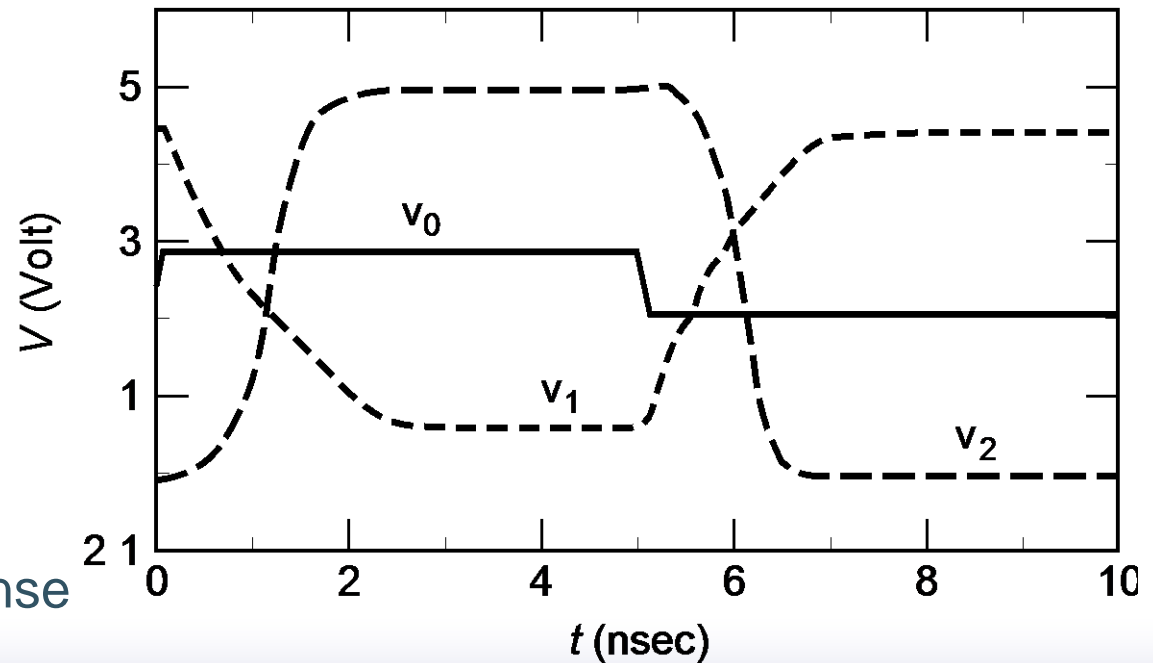


Non-Regenerative

# Regenerative Property

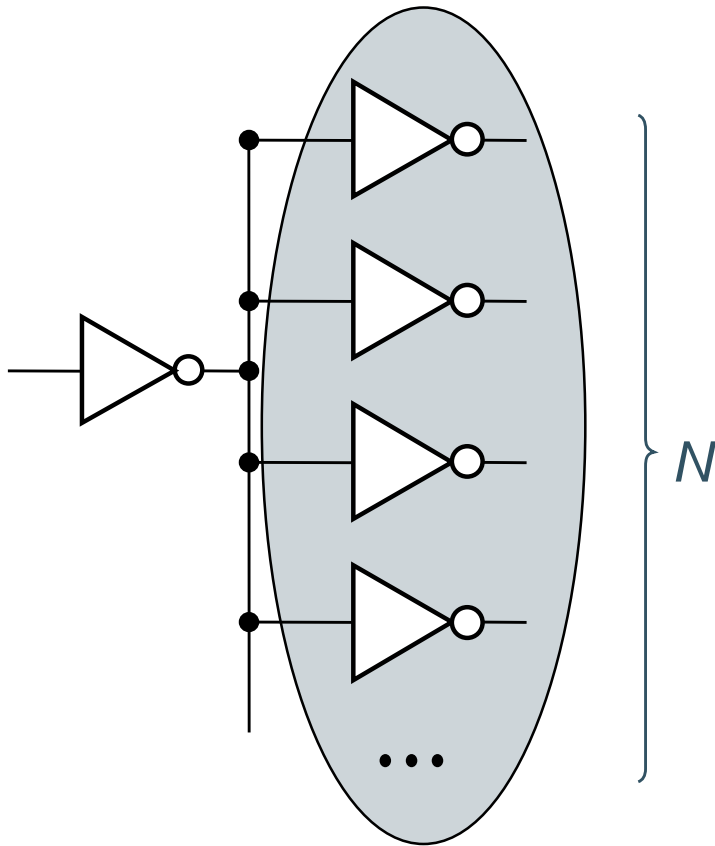


A chain of inverters

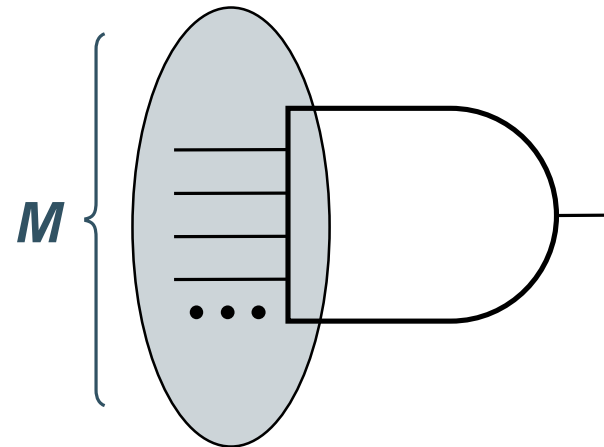


Simulated response

# Fan-in and Fan-out



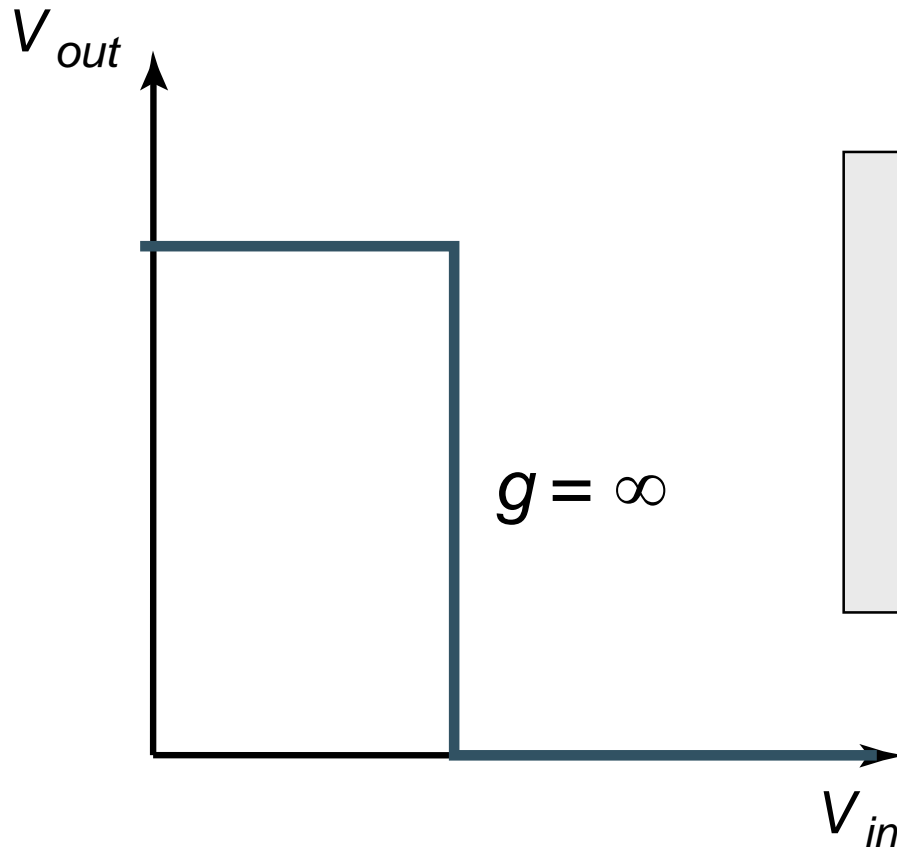
Fan-out  $N$



Fan-in  $M$



# The Ideal Gate



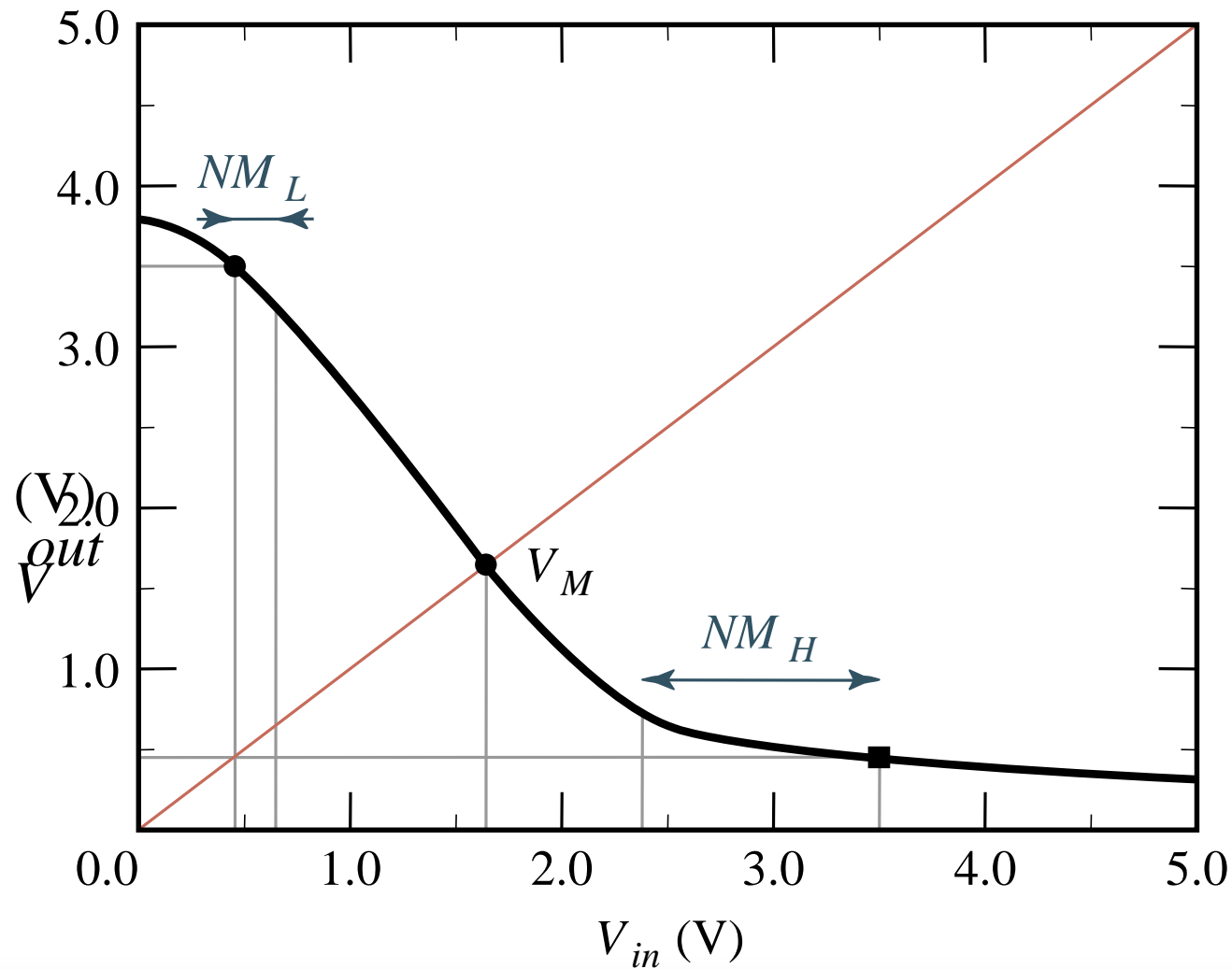
$$R_i = \infty$$

$$R_o = 0$$

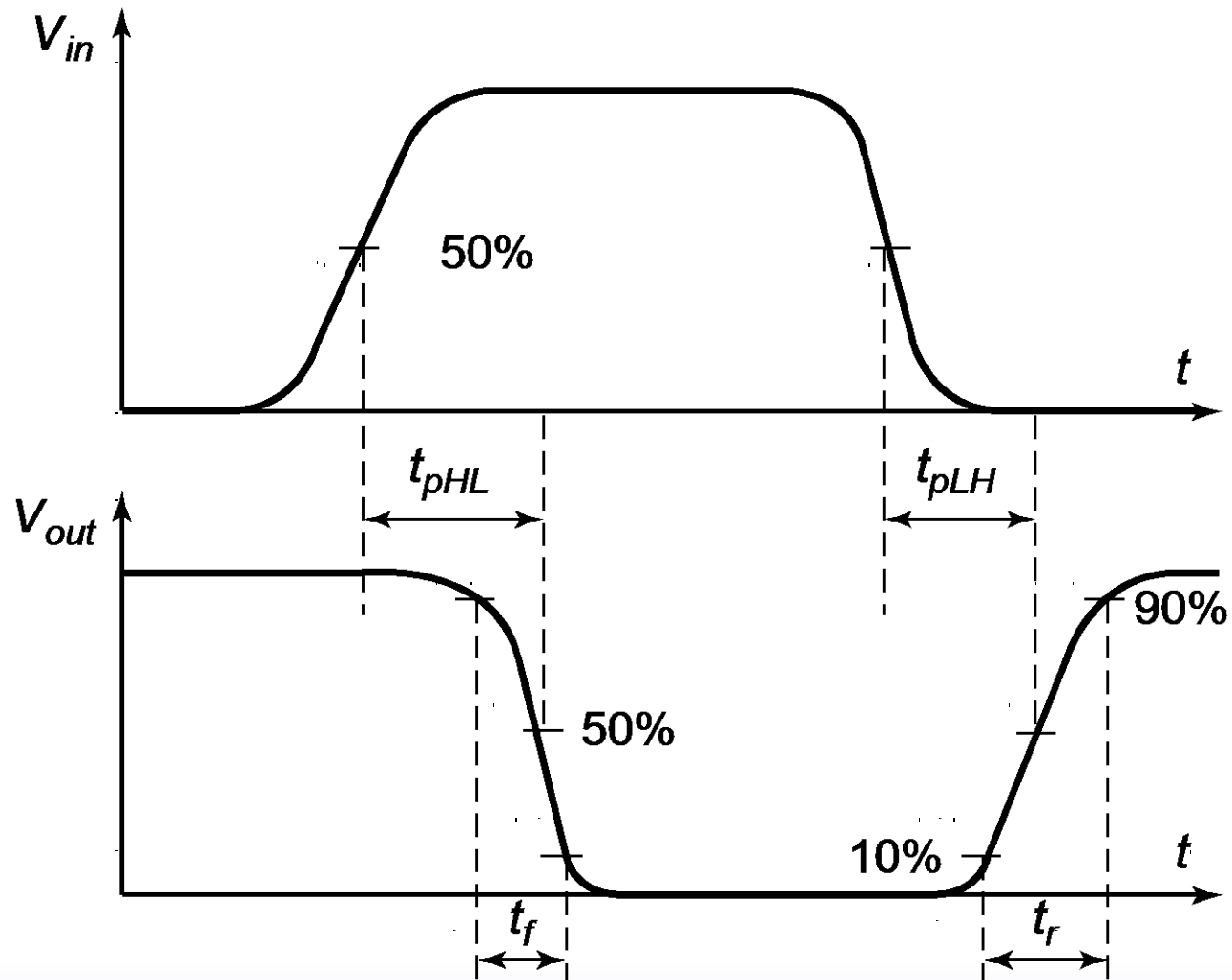
$$\text{Fanout} = \infty$$

$$NM_H = NM_L = V_{DD}/2$$

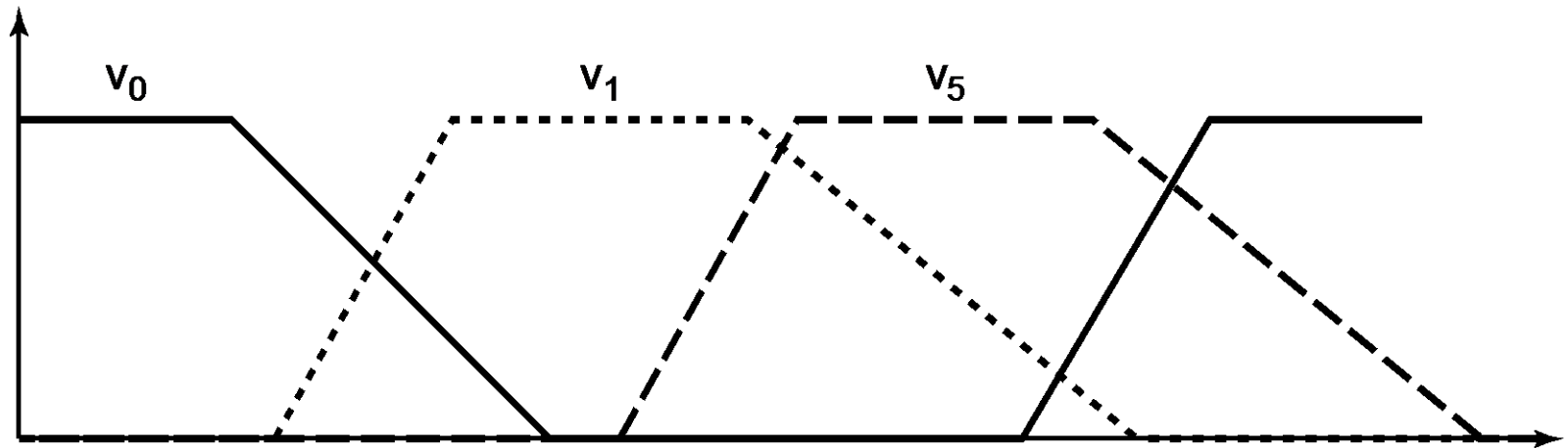
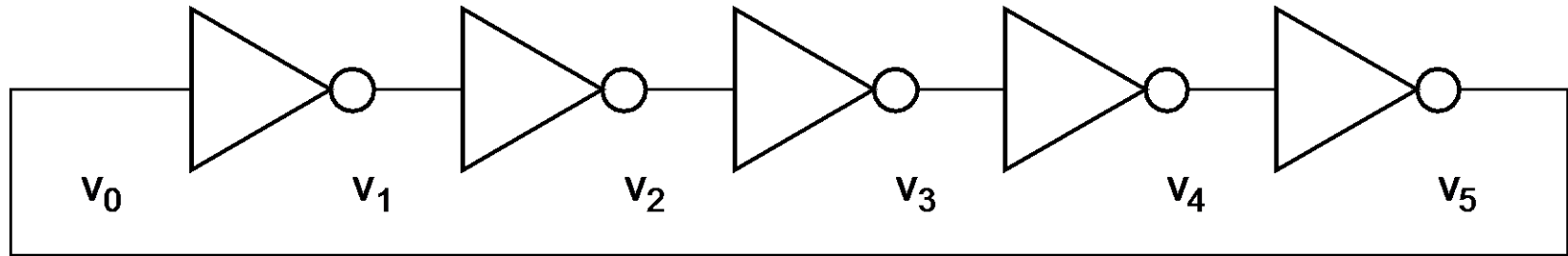
# An Old-time Inverter



# Delay Definitions

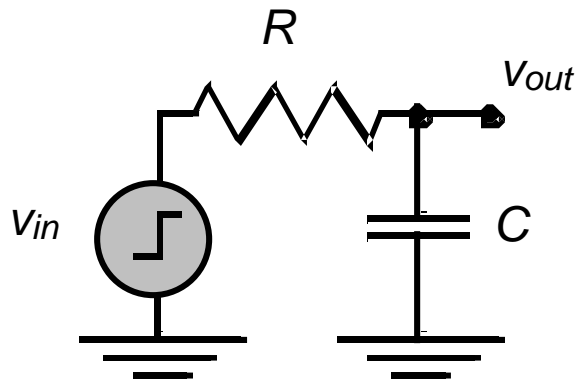


# Ring Oscillator



$$T = 2 \times t_p \times N$$

# A First-Order RC Network



$$v_{out}(t) = (1 - e^{-t/\tau}) V$$

$$t_p = \ln(2) \tau = 0.69 RC$$

Important model – matches delay of inverter

# Power Dissipation

Instantaneous power:

$$p(t) = v(t)i(t) = V_{supply}i(t)$$

Peak power:

$$P_{peak} = V_{supply}i_{peak}$$

Average power:

$$P_{ave} = \frac{1}{T} \int_t^{t+T} p(t)dt = \frac{V_{supply}}{T} \int_t^{t+T} i_{supply}(t)dt$$

# *Energy and Energy-Delay*

Power-Delay Product (PDP) =

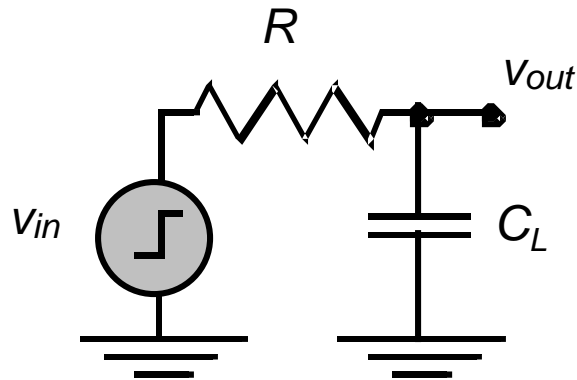
$$E = \text{Energy per operation} = P_{av} \times t_p$$

Energy-Delay Product (EDP) =

$$\text{quality metric of gate} = E \times t_p$$



# A First-Order RC Network



$$E_{0 \rightarrow 1} = \int_0^T P(t) dt = V_{dd} \int_0^T i_{supply}(t) dt = V_{dd} \int_0^{V_{dd}} C_L dV_{out} = C_L \cdot V_{dd}^2$$

$$E_{cap} = \int_0^T P_{cap}(t) dt = \int_0^T V_{out} i_{cap}(t) dt = \int_0^{V_{dd}} C_L V_{out} dV_{out} = \frac{1}{2} C_L \cdot V_{dd}^2$$

# Summary

- ❑ Digital integrated circuits have come a long way and still have quite some potential left for the coming decades
- ❑ Some interesting challenges ahead
  - Getting a clear perspective on the challenges and potential solutions is the purpose of this book
- ❑ Understanding the design metrics that govern digital design is crucial
  - Cost, reliability, speed, power and energy dissipation